Nonfundamental Asset Price Fluctuations and the Distributional Origins of Asset Premia*

Fabio Stohler†
University of Bonn

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Abstract

This paper investigates why different asset classes earn different premia. To answer this, I build and estimate a heterogeneous-agent business-cycle model with incomplete markets, portfolio choice, and nonfundamental asset price shocks. The estimated model successfully matches empirical equity and term premia. Household heterogeneity is key, as limited risk sharing leads the households that bear aggregate risk to demand sizable compensation. The model shows that half of the equity premium arises from fundamental macroeconomic shocks, while the other half compensates for risks from nonfundamental asset price fluctuations. Term premia are driven by monetary policy shocks at short maturities and by persistent technology shocks at longer maturities. While nonfundamental asset price shocks play a prominent role in the equity premium, they have limited effects on aggregate outcomes and inequality. Finally, I use the model to explain time variation in asset premia and to assess how monetary policy shapes their level over time.

Keywords: Incomplete Markets, Asset Pricing, Business Cycles, Monetary Policy
JEL codes: D31, D52, E44, E52, G12

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†Web: https://fabio-stohler.github.io/, Email: fabio.stohler@uni-bonn.de.

1 Introduction

A central puzzle in financial economics is that risky asset prices exhibit much greater volatility than their fundamentals (Shiller, 1981). A prominent explanation for this, dating back to Keynes (1936), is that interactions among traders, driven by "animal spirits," can push asset prices away from fundamental values. This volatility matters for macroeconomic analysis, as a growing empirical literature shows that fluctuations in asset prices generate sizable demand-side effects (e.g., Pflueger, Siriwardane and Sunderam, 2020, Chodorow-Reich, Nenov and Simsek, 2021). Hence, when "animal spirits" drive asset prices, financial markets can act as an independent source of fluctuations.

A related, but distinct, economics literature has asked to what extent macroeconomic fluctuations and inequality can explain asset premia, or whether they are themselves a hard-to-rationalize "animal spirits" phenomenon (see Mehra, 2012 and Shiller, 2014). My paper contributes to this literature. To this end, I develop and estimate a quantitative heterogeneous-agent New Keynesian business-cycle model with endogenous portfolio choice, in which equilibrium equity prices respond to fundamental macroeconomic shocks and a nonfundamental asset price shock.

The estimated model yields quantitative asset pricing implications that closely align with U.S. data. It reproduces empirical equity and term premia, generating an equity premium of 4.92 percent and an upward-sloping yield curve with term premia of 0.24 and 1.71 percent for 1- and 10-year bonds, respectively. The magnitude of these premia reflects households' limited ability to share aggregate risk in the presence of incomplete markets and realistic inequality. In this environment, even moderate risk aversion is sufficient for households to demand sizable premia in compensation for aggregate risk.

Decomposing asset premia shows that nonfundamental asset price risk accounts for nearly half of the equity premium. At the same time, monetary policy shocks account for most of the short-maturity term premium, while persistent technology shocks account for the long-maturity component. Despite its importance for equity prices, the nonfundamental shock has little effect on macroeconomic aggregates or inequality. Instead, technology and markup shocks explain the majority of the business-cycle fluctuations.

I use the model to study the impact of changes in aggregate risk and monetary policy on asset premia. First, I re-estimate the model over the post-Volcker and post-2000 periods and show that it can explain the time variation in asset premia through changes in the shock structure and declining macroeconomic volatility. Second, the model indicates that stronger monetary policy responses to inflation increase the premia households demand since they face larger aggregate fluctuations caused by supply-side shocks.

In more detail, I built a structural heterogeneous-agent New Keynesian model with the following key features. The household side builds on the one-asset framework of Auclert, Rognlie and Straub (2025), which I extend to incorporate portfolio choice and asset pricing, following the methodology of Auclert et al. (2024). Households face idiosyncratic risk and have access to incomplete financial markets, so they cannot insure themselves fully against idiosyncratic income fluctuations. They hedge aggregate risk by forming a portfolio of bonds with different maturities, physical capital, and an equity fund. In equilibrium, they demand asset premia on all assets to compensate for utility fluctuations induced by aggregate risk.

This household block is integrated into the quantitative New Keynesian business-cycle environment of Christiano, Eichenbaum and Evans (2005) and Smets and Wouters (2007), which features several nominal and real frictions. On the production side, wholesale firms accumulate capital subject to investment adjustment costs. Their output is then differentiated by retail firms, which face Calvo-style price stickiness with partial inflation indexation. The labor market exhibits similar rigidities, with unions setting wages under Calvo contracts that are also partially indexed. The government finances expenditures through taxes and multi-maturity bond issuance, and a central bank sets the nominal interest rate via a Taylor rule responding to inflation and output growth.

Given evidence that significant, yet-to-be-quantified, shares of asset price movements are nonfundamental, my model also allows for these shocks. I follow De Long et al. (1990) and model equilibrium equity prices as the result of the interaction of fundamental traders and noise traders in segmented financial markets.[1] Fundamental traders value equities based on discounted fundamentals, while noise traders generate unpredictable shifts in equity demand unrelated to fundamentals. Equilibrium prices reflect both the fundamental demand and the nonfundamental demand of noise traders, leading to deviations of equity prices from their fundamental values.[2] Markets are segmented so that households cannot trade individual equities directly. Instead, they can only invest in an aggregate equity index fund that tracks the value of all individual equities. Through their holdings of this index fund, households become exposed to nonfundamental asset price fluctuations originating from noise traders.

[1] Seminal contributions that feature nonrational noise traders include Kyle (1985) and Campbell and Kyle (1993). More recent applications of noise traders in exchange rate markets are Gabaix and Maggiori (2015), Itskhoki and Mukhin (2021), Fukui, Nakamura and Steinsson (2023), and Itskhoki and Mukhin (2025), among others.

[2] In addition to microfounding nonfundamental asset price fluctuations through noise traders, I derive an alternative derivation based on incomplete information in the style of Futia (1981) and Singleton (1986) that yields an identical reduced-form pricing equation to first order.

I bring the model to the data in two steps. First, I calibrate the model to match time series averages of macroeconomic variables, the wealth and income distributions, and the aggregate marginal propensities to consume out of labor income. Next, I estimate the parameters governing aggregate dynamics using Bayesian methods on macroeconomic and financial time series. Notably, the level of asset premia remains untargeted, allowing the model-implied premia to be used for model validation.

The estimated model closely reproduces the untargeted empirical equity and term premia. I compute these premia following Auclert et al. (2024), which allows me to obtain asset premia from a model solved only to first-order by using a second-order approximation to portfolio choice. Applying this approach to the estimated model yields an equity premium of 4.92 percent per year, which is broadly consistent with the empirical estimate of 5.01 percent per year. The model-implied yield curve also aligns well with the data. The average annual term premia for one- and ten-year bonds are 0.24 and 1.71 percent, close to their empirical counterparts of 0.36 and 1.77 percent.

The intuition for the model's large asset premia boils down to limited risk-sharing. Households can trade different assets, but significant wealth and income inequality limit aggregate risk sharing. Most households have little savings, leaving them highly exposed to idiosyncratic risk. If these households buy assets, they desire to hold safe assets with low return volatility, such as short-term bonds, that can be used for consumption smoothing after a negative idiosyncratic shock. In contrast, the few wealthy households that are best insured against idiosyncratic risk become the primary owners of risky assets such as equity and long-term bonds. Crucially, this small group of wealthy households must absorb all aggregate risk. Their consumption is thus disproportionately exposed to aggregate risk. While well-insured against idiosyncratic risk, these households demand a premium in line with standard consumption-based asset pricing: the risk premium is high because asset returns covary positively with their intertemporal marginal rate of substitution. This intuition is confirmed by a counterfactual exercise using a complete-market, representative agent model. In that setting, all households in the economy are perfectly insured against idiosyncratic risk and share aggregate risk equally. With aggregate risk equally shared, there is little covariation between the intertemporal marginal rate of substitution and returns, and all asset premia become negligible.

I can decompose the model-implied asset premia into the contributions of individual structural shocks. 45 percent of the equity premium is compensation for exposure to nonfundamental asset price risk, while the remaining 55 percent is compensation for fundamental business-cycle risk. For the one-year bond, 65 percent of the term premium is explained by monetary policy shocks. In contrast, for the ten-year bond, almost 80

percent is explained by investment-specific technology shocks.

The risk-sharing intuition also explains the main contributors to the equity premium and the term premia across different maturities. Equity is held almost exclusively by wealthy households, who are uniquely exposed to nonfundamental asset price shocks. Despite low MPCs, the resulting return volatility creates a sizable positive covariance between their consumption and equity returns, making the asset risky for them and requiring a premium. Note that while fundamental risk explains a significant fraction of the equity premium in this model, the nonfundamental asset price shock is essential to generate the realistic equity premium. Similar logic explains the term premium. Wealthy households also hold long-maturity bonds, where persistent technology shocks create a positive covariance between their consumption and long-bond returns, again requiring a term premium. In contrast, short-term bonds are held by less wealthy, often constrained households. For this group, monetary policy-driven returns exhibit weak covariance with consumption. This lack of risk commands a lower premium, generating an upward-sloping term premium.

After analyzing asset premia through the model, I can investigate the impact of nonfundamental asset price shocks on aggregate variables, thereby determining whether asset price fluctuations are an important source of macroeconomic fluctuations. The model attributes roughly two-thirds of the empirical equity return volatility to nonfundamental sources. Yet, the effects of nonfundamental asset price fluctuations on other macroeconomic aggregates and inequality are modest. The nonfundamental asset price shock accounts for 7.8 percent of the variance in consumption growth at the business-cycle frequency, while technology shocks still explain the bulk of the variance. In terms of distributional consequences, a positive nonfundamental shock raises the value of wealth for households at the top of the distribution, thereby increasing wealth inequality. Quantitatively, however, this effect is small: nonfundamental asset price shocks account for only 6.2 percent of the variance in the Gini coefficient of wealth.

To clarify the intuition behind the limited impact of the nonfundamental asset price shock on aggregates and inequality, two mechanisms are central. First, equity comprises only about one-fifth of total household assets. As a result, even large movements in equity prices induce relatively modest changes in aggregate household wealth. Second, the aggregate marginal propensity to consume (MPC) from total wealth is low, as high-wealth, low-MPC households hold most of it. As a result, fluctuations in asset values translate only weakly into changes in aggregate consumption. Together, these factors imply that although nonfundamental shocks drive asset price volatility, they have muted effects on macroeconomic aggregates such as consumption.

A similar logic applies to the limited role of nonfundamental asset price shocks in explaining wealth inequality. While they primarily affect a few wealthy households, who hold disproportionate shares of risky assets, their overall impact on wealth distribution remains small. This is because the model's primary sources of redistribution stem from shocks with broader macroeconomic consequences, such as technology, investment-specific technology, and government expenditure shocks that impact the majority of households. As a result, nonfundamental shocks have limited power in shaping inequality dynamics relative to other sources of economic risk.

Finally, I use the model to examine how time-varying aggregate risk and monetary policy shape asset premia. When re-estimated for the post-Volcker and post-2000 periods, the model matches the empirical variation in asset premia. In line with the increased macroeconomic volatility during the first period, the model produces higher asset premia in this same period. In other words, the model also provides a microfoundation for time-varying asset premia. When studying the effect of monetary policy on asset premia, I show that more hawkish monetary policy, in the sense of stronger inflation targeting, increases asset premia. Over the estimation period, the model attributes most of the time series variation in aggregates to supply-side shocks. As a result, a more hawkish monetary policy lowers inflation volatility while raising macroeconomic volatility. Because households are exposed to greater macroeconomic risk, they demand a higher premium.

Related Literature: This paper contributes to several branches of the macro-finance literature. First, it relates to the extensive literature that tries to explain the equity premium puzzle (Mehra and Prescott, 1985, Weil, 1989) and the term premium puzzle (Backus, Gregory and Zin, 1989, Cochrane and Piazzesi, 2005). Within this vast field,[3] it contributes in particular to the literature on consumption-based asset pricing with heterogeneous agents (see Constantinides and Duffie, 1996, Krusell and Smith, 1997, Storesletten, Telmer and Yaron, 2007, Guvenen, 2009, Krueger and Lustig, 2010, Krusell, Mukoyama and Smith, 2011, and Constantinides and Ghosh, 2017, among others). Closely related to my work is Auclert et al. (2024). They analyze how portfolio choice affects aggregate dynamics and show that a tractable heterogeneous-agent New Keynesian model still generates an equity premium puzzle. In contrast, I show that household heterogeneity is central for explaining asset premia. Calibrating the joint distribution of income and wealth to match U.S. inequality, I find that limited risk sharing among households leads those who bear aggregate risk to demand sizable premia to

[3] Referencing all contributions is not feasible here. See Cochrane (2008) and Mehra (2012) for reviews.

hold risky assets. This mechanism drives my main quantitative contribution. To the best of my knowledge, this is the first paper to calibrate and estimate a heterogeneous-agent New Keynesian business cycle model and to conduct asset pricing with an equally rich asset structure.

The results also speak to the macro-finance literature that decomposes asset premia using estimated models (see Bansal and Yaron, 2004, Hansen, Heaton and Li, 2008, Rudebusch and Swanson, 2012, and Schorfheide, Song and Yaron, 2018, Campbell, Pflueger and Viceira, 2020). While these studies provide valuable decompositions, their main distinction is between short-run and long-run risk rather than by structural source. In contrast, this paper decomposes asset premia into contributions from specific macroeconomic shocks. This allows me to study how changes in the shock structure and monetary policy impact asset premia. Consistent with the existing literature, I find that persistent shocks account for a large share of asset premia. However, I also show that short-term nonfundamental fluctuations are essential for explaining the equity premium.

Moreover, the paper advances research on how asset price fluctuations affect macroeconomic aggregates and inequality. Recent work has examined the wealth effect of asset price movements on consumption (Gali, 2014, Caballero and Simsek, 2020, Kaplan, Mitman and Violante, 2020, Chodorow-Reich, Nenov and Simsek, 2021, Gali, 2021), on investment through the alleviation of credit constraints (Dupor, 2005, Martin and Ventura, 2012, Miao and Wang, 2018, Pflueger, Siriwardane and Sunderam, 2020), and on inequality and household welfare (Glover et al., 2020, Kuhn, Schularick and Steins, 2020, Cioffi, 2021, Fernández-Villaverde and Levintal, 2024, and Fagereng et al., 2025). This paper complements that work by analyzing these effects in an estimated general equilibrium New Keynesian model with heterogeneous agents and endogenous portfolio choice. The structural framework allows me to quantify the impact of asset price fluctuations on aggregate variables, asset premia, and inequality within a general equilibrium framework, and to identify and decompose the channels through which these fluctuations operate. There is some overlap of my work with Gong (2025a), who analyzes the transmission of asset price changes to household consumption in a heterogeneous-agent economy. However, the two papers crucially differ in where the information friction that generates the nonfundamental asset price fluctuations applies. I take a conservative approach that confines the information friction leading to nonfundamental asset price movements to the financial sector. In contrast, he assumes that households do not observe the risk-free rate and thus misinterpret asset price movements from discount rate shocks as increases in wealth, thereby generating large wealth effects. Based on my conservative assumptions, I find that nonfundamental asset price movements have only

a modest impact on macroeconomic aggregates and inequality.

Finally, this paper contributes to the literature examining macroeconomic fluctuations using estimated quantitative macroeconomic models. My estimation results broadly align with those from estimated representative agent models (Christiano, Eichenbaum and Evans, 2005, Smets and Wouters, 2007, Justiniano, Primiceri and Tambalotti, 2011, Boehl, 2022) and heterogeneous agent models (Auclert, Rognlie and Straub, 2020, Bayer, Born and Luetticke, 2022, Boehl, 2024, Bayer, Born and Luetticke, 2024). In my framework, supply-side shocks account for most of the variation in aggregate variables and inequality measures at business-cycle frequencies. The key exception is equity prices, whose movements are chiefly driven by the novel asset price shock. However, introducing the asset price shock does not fundamentally change our understanding of the main forces behind business cycle fluctuations.

Outline: The remainder of the paper is organized as follows: Section 2 describes the model, Section 3 discusses the calibration and Bayesian estimation of the model. Section 4 presents the model-implied asset premia, decomposes the premia, and explains them through household heterogeneity. Section 5 studies the impact of the asset price shocks on macroeconomic aggregates and inequality. Section 6 uses the model to examine asset premia across different periods and the effect of monetary policy on them. Section 7 concludes. The Appendix contains all proofs omitted from the main text, an extensive illustration of the data used, and details of the estimation results for each parameter.

2 HANK Model with Nonfundamental Asset Price Shocks

This section presents a heterogeneous-agent New Keynesian (HANK) model that incorporates household portfolio choice, segmented financial markets, and nonfundamental asset price fluctuations. Households choose between equity, capital, and government bonds of varying maturities to self-insure against idiosyncratic income risk and to hedge exposure to aggregate shocks. Risk premia arise endogenously as households demand premia in compensation for utility fluctuations induced by macroeconomic risk. The financial sector features a segmented equity market, as households can only trade in an equity fund. Fundamental traders interact with noise traders so that equilibrium asset prices reflect changes in asset payoffs and nonfundamental changes in noise traders' expectations. Any asset price fluctuations are transmitted to households indirectly through an index fund that intermediates between traders and household investors. I embed this financial structure into a quantitative general equilibrium framework with standard

New Keynesian frictions in pricing, capital adjustment costs, and wage setting, following Christiano, Eichenbaum and Evans (2005) and Smets and Wouters (2007). The government issues bonds of different maturities and conducts fiscal policy through taxes and government consumption, while monetary policy follows a standard Taylor rule.

2.1 Nonfundamental Asset Price Shocks in the Equity Market

The equity market model builds on De Long et al. (1990) and Gabaix and Maggiori (2015).[4] The market is segmented in the sense that households do not trade individual equities directly, but instead invest exclusively in an equity index fund. Three types of agents operate in the equity market: fundamental traders, noise traders, and an equity fund that intermediates between them and households. I assume a unit continuum of traders indexed by $l \in [0,1]$, of which a measure ν are fundamental traders ($l \in [0,\nu]$) and a measure $1-\nu$ are noise traders ($l \in (\nu,1]$). All traders live for two periods: they purchase a portfolio of assets in the first period and earn returns in the second. Since the equity fund owns traders, it finances their purchases with revenues collected from household investments and returns the profits traders earn to the fund, which are ultimately passed on to households. Both types of traders trade a continuum of individual equities indexed by $j \in [0,1]$, each issued by a retail firm. Individual equity prices are determined in equilibrium through market clearing. The index fund aggregates these equities into a diversified portfolio and sells shares of the fund to households.

Fundamental Traders: Each fundamental trader is risk-neutral,[5] derives utility from the profits of their equity portfolio, discounts future cash flows at the risk-free rate $1 + r_{t+1}$, and incurs quadratic disutility from monitoring firm-specific fundamentals, which increases with the size of the trader's net position. The disutility follows Angeletos and Lian (2016) and is motivated by the higher cognitive costs traders incur when they must closely monitor large portfolio positions. Each fundamental trader $l \in [0,\nu]$ chooses a portfolio allocation $\{\theta_{ljt}\}_{j\in[0,1]}$ to maximize utility U_{lt}:

$$U_{lt} = \max_{\{\theta_{ljt}\}} \int_0^1 \left[-q_{jt}^{eq}\theta_{ljt} + \mathbb{E}_t\left(\frac{d_{jt+1}+q_{jt+1}}{1+r_{t+1}}\right)\theta_{ljt} - \frac{1}{2}\theta_{ljt}^2 \right] dj,$$

[4] In Appendix I, I derive an alternative formulation based on incomplete information that yields the same reduced-form equilibrium asset price.

[5] I can also integrate limits to arbitrage by assuming that fundamental traders are risk averse according to a CARA utility function as in De Long et al. (1990), or Bacchetta and Wincoop (2006).

where d_{jt} and q_{jt}^{eq} denote the dividend and price of equity j, respectively. The functional form yields a linear demand schedule for each equity:

$$\theta_{ljt} = -q_{jt}^{eq} + \mathbb{E}_t \left[\frac{d_{jt+1} + q_{jt+1}}{1 + r_{t+1}} \right] \quad \forall\, l \in [0, \nu]. \tag{1}$$

Noise Traders: Noise traders represent the second group of market participants. Unlike fundamental traders, their investment behavior is unrelated to economic fundamentals. This may reflect behavioral motives or non-rational stock-picking strategies. Specifically, the demand of each noise trader for stock j is given by:

$$\theta_{ljt} = \tilde{\xi}_t + \epsilon_{ljt}^{\theta},$$

where $\tilde{\xi}_t$ is an aggregate noise-trader demand component and ϵ_{ljt}^{θ} is an idiosyncratic, iid shock to the noise trader–stock j demand.

Equity Fund: The fund aggregates all equities into a single index, which households can invest in. The fund finances trader purchases using household contributions, collects dividends and capital gains from traders' equity holdings, and distributes the resulting returns back to households. I assume that the fund weights all equities equally, such that the price of the index fund equals the average price of the underlying equities and pays the average of the underlying dividends:

$$q_t^{eq} = \int_0^1 q_{jt}^{eq} dj, \qquad d_t = \int_0^1 d_{jt} dj.$$

Equilibrium Asset Prices: In equilibrium, the aggregate demand for each equity must equal its supply (normalized to one), implying: $\int_0^1 \theta_{ljt} dl = 1$. In Appendix I I illustrate that this market-clearing condition implies that the price of equity j is:

$$q_{jt}^{eq} = \mathbb{E}_t \left[\frac{d_{jt+1} + q_{jt+1}}{1 + r_{t+1}} \right] + \xi_t, \tag{2}$$

where the effective asset price shock is defined as $\xi_t \equiv \frac{(1-\nu)\tilde{\xi}_t - 1}{\nu}$, and follows an AR(1) process $\xi_t = \rho_q \xi_{t-1} + \epsilon_t^q$, where $\epsilon_t^q \sim \mathcal{N}(0, \sigma_q^2)$. This formulation makes the role of nonfundamental fluctuations explicit and facilitates their estimation. In a symmetric

equilibrium where all equities are identical,[6] the aggregate index fund price is:

$$q_t^{eq} = \mathbb{E}_t \left[\frac{d_{t+1} + q_{t+1}}{1 + r_{t+1}} \right] + \xi_t. \tag{3}$$

Hence, the common noise trader demand component shifts the entire equity price level, thereby increasing market valuation even when fundamentals remain unchanged.

2.2 Household Sector with Portfolio Choice and Asset Pricing

The household side of the model combines a standard consumption–savings problem with idiosyncratic income risk and incomplete markets with portfolio choice to hedge against aggregate fluctuations. Households earn net labor income, accumulate assets to self-insure against idiosyncratic shocks, and allocate their portfolios across available assets to mitigate exposure to aggregate risk.

Idiosyncratic Risk: There is a continuum of households indexed by $i \in [0, 1]$, which are ex-ante identical but differ ex-post due to uninsurable idiosyncratic risk in their labor efficiency e_{it} and their patience, captured by their discount factor $\tilde{\beta}_{it}$. A Markov Chain describes the transitions between an individual state $(e_{it}, \tilde{\beta}_{it})$ and any other state $(e_{it+1}, \tilde{\beta}_{it+1})$. I assume that the labor productivity and discount factor processes are independent, and the mass of agents in each state is always equal to the mass in the stationary distribution. I assume that there are two realizations of the discount factor: a high discount factor β^H for patient households and a low discount factor $\beta^L = \beta^H - \Delta^\beta$ for relatively impatient households. Each period, with probability ϖ a household obtains a new draw of the discount factor, where the probability for transmitting into either of the two patience states is equal to the stationary distribution of the respective states $(\omega, 1 - \omega)$, where ω denotes the fraction of patient households in the stationary distribution economy. Finally, I normalize the cross-sectional mean of labor productivity to unity $\int_0^1 e_{it} di = 1$.

Household problem: Households can save in $K+1$ assets, subject to a zero-borrowing constraint on their total portfolio wealth, and earn labor income, which is taxed at a rate τ_t. Households have Epstein-Zin preferences over their felicity from consumption c_{it} and labor n_{it}. $1/\rho$ denotes the intertemporal elasticity of substition and γ denote the risk-aversion parameter of households. Households have King, Plosser and Rebelo (1988)

[6] I assume that all retail firms are symmetric. As a result, their equities have identical payoffs, which implies by equation (2) that equity prices are also identical. Thus, all equities are identical.

utility and obtain utility from consumption, but dislike supplying labor n_{it}, according to $v(\cdot)$. The problem of household i in period t, with idiosyncratic income productivity e_{it}, idiosyncratic discount factor β_{it}, and with portfolio holdings $\{a_{it}^k\}_{k=0}^K$, where a_{it}^k denotes their portfolio holding of asset $k \in [0, 1, ..., K]$ is given by:

$$V_{it} = \max_{\{c_{it}, n_{it}, \{a_{it}^k\}_{k=0}^K\}_{t=0}^\infty} \left((1-\beta_{it}) \left(c_{it} e^{-v(n_{it})} \right)^{1-\rho} + \beta_{it} \left(\mathbb{E}_t \left[V_{it+1}^{1-\gamma} \right] \right)^{\frac{1-\rho}{1-\gamma}} \right)^{\frac{1}{1-\rho}} \tag{4}$$

$$\text{s.t.} \quad c_{it} + \sum_{k=0}^{K} q_t^k a_{it}^k \leq \sum_{k=0}^{K} \left(q_t^k + x_t^k \right) a_{it-1}^k + e_{it}(1-\tau_t) w_t n_{it}, \tag{5}$$

$$\text{and} \quad \sum_{k=0}^{K} q_t^k a_{it}^k \geq 0. \tag{6}$$

The household's time-varying discount factor is defined as $\beta_{it} \equiv \tilde{\beta}_{it}\zeta_t$, where $\tilde{\beta}_{it}$ is the idiosyncratic component, and ζ_t is an aggregate discount factor shock. The aggregate component ζ_t evolves according to a log-linear AR(1) process with persistence ρ_ζ and innovation $\epsilon_\zeta \sim \mathcal{N}(0, \sigma_\zeta^2)$. In the household budget constraint (5), q_t^k and x_t^k denote the price and payoff of asset k, respectively. I assume that households allocate wealth across a menu of nine assets: equity, capital, and government bonds with seven different maturities. The pre-tax real wage per unit of efficient labor is denoted by w_t; however, individual households do not choose their own hours worked; instead, labor supply is determined collectively by unions in response to current labor demand.

Representative Agent Benchmark: I also solve a version with a representative household. The household faces the same maximization problem as in equations (4–6), but with homogeneous labor income $e_{it} = 1$ and a common, time-varying discount factor $\beta_{it} = \beta_t$.

Solving for Optimal Portfolios and Risk Premia: I solve the model using the sequence-space approach of Auclert et al. (2021), modeling aggregate shocks as first-order "MIT shocks": the economy is perturbed by unanticipated shocks at date $t = 0$, after which all future periods evolve under perfect foresight. In this deterministic environment, all assets yield equal expected returns from period $t > 0$ onward, rendering households locally indifferent across assets and leaving portfolio choices indeterminate. However, at $t = 0$, realized shocks induce variation in ex-post returns, thereby making the portfolio problem well-defined. Tille and Wincoop (2010) and Devereux and Sutherland (2011) develop a method to recover optimal portfolio allocations and associated risk premia in

this setting, which Auclert et al. (2024) extend to a heterogeneous agent environment. I follow their approach and offer a brief overview of the intuition and key equations below. A more detailed illustration of the method is provided in Appendix II.

The core idea is that households, anticipating the economy's response to aggregate shocks, know their utility exposure to aggregate shocks and how asset returns change in period 0. Given this information, households take asset positions in period -1 to hedge against fluctuations in utility. By imposing market-clearing across all individual assets, the method jointly determines equilibrium portfolio positions, households' exposures to aggregate risk, and the corresponding risk premia that compensate households for bearing this risk.

Portfolio Choice: This section describes how households choose asset holdings a_i^k across $K+1$ assets in a linearized environment. Let $\boldsymbol{\epsilon}$ be the vector of Z aggregate shocks, let $R^k(\boldsymbol{\epsilon})$ denote the state-dependent gross return on asset k, and let $W_i \equiv \left(\mathbb{E}_t[V_{it}^{1-\gamma}]\right)^{\frac{1}{1-\gamma}}$ denote the value function after integrating out idiosyncratic income risk. Assuming that portfolio constraints do not bind, the optimal choice between asset k and a reference asset 0 is characterized by

$$\sum_{z=1}^{Z}\left(\frac{\partial \log R^k(\boldsymbol{\epsilon})}{\partial \epsilon_z} - \frac{\partial \log R^0(\boldsymbol{\epsilon})}{\partial \epsilon_z}\right)\frac{d\log W_i'}{d\epsilon_z}\sigma_z \;=\; b^k, \tag{7}$$

where the summation over shocks is equal to the expectation operator over aggregate shocks in the linearized environment, primes indicate derivatives, b^k corresponds to the negative of the premium on asset k relative to asset 0, and σ_z is the standard deviation of a shock z. Equation (7) states that households choose portfolios so that, in expectation, the product of marginal utility and the return differential does not fluctuate after aggregate shocks. Equation (7) represents the linearized counterpart of the portfolio-choice optimality condition that arises in globally solved models.

Auclert et al. (2024) show that in a linearized economy, if there are at least as many linearly independent assets as aggregate shocks ($K \geq Z$), asset markets are complete with respect to aggregate risk. Market completeness means that, through trade in assets, all households share the same exposure of marginal utility to each shock:

$$\frac{d\log W_i'}{d\epsilon_z} = \lambda_z \quad \forall i. \tag{8}$$

Although equation (8) implies that all households have the same exposure to each shock, this does not imply that households have full insurance against aggregate risk. In equi-

librium, market-clearing may limit risk sharing among households. If all households are adversely affected by aggregate shocks, aggregate risk cannot be diversified away, leading to less than full insurance. As a result, households bear residual aggregate risk with exposures λ_z that are pinned down by the distribution of marginal utility responses across households to aggregate shocks.

For my quantitative application, I allow households to choose portfolios that deliver the risk-sharing allocation characterized by equation (8), subject to market clearing. In equilibrium, the households that hold positive net positions in an asset are those that, before trading in assets in anticipation of shocks, are least affected in utility terms by the aggregate shocks that move the asset's return.[7] Examining how these net holders respond to a shock will later be useful to clarify the residual exposure to the aggregate risk that they bear. My assumption that portfolio constraints do not bind may overstate the degree of insurance households can obtain and understate the required compensation for risk. This implies that the model's implied risk premia represent a lower bound.[8]

Risk Premia: Because households cannot fully insure against aggregate risk, they demand a premium for bearing residual aggregate exposures. The methodology provides a closed-form approximation of the corresponding average risk premia.[9] For any asset k, its premium relative to the reference asset 0 is approximately

$$\frac{R^k(\sigma) - R^0(\sigma)}{R} \approx -\sum_{z=1}^{Z} X_{zk}\lambda_z\overline{\sigma}_z^2\sigma^2 = -b^k, \tag{9}$$

where X_{zk} measures the sensitivity of asset k's return to shock z, and λ_z captures the average exposure of marginal utility from equation (8). Together, X_{zk} captures how payoffs load on shocks and λ_z captures the equilibrium exposure of marginal utility, so

[7] Note that these households still benefit from trading because the exchange of state contingent payoffs shifts income toward states where their marginal utility is high and away from states where it is low.

[8] Auclert et al. (2024) shows how to compute constrained optimal portfolios in the case of two assets. Extending this to settings with more assets, such as the nine asset setup considered here, is more challenging. They note that imposing portfolio constraints tends to push results toward those implied by exogenous portfolio rules, for example, constant shares, typically increasing the level of risk premia while reducing the extent of endogenous insurance. Importantly, they find limited effects on aggregate dynamics. Consequently, my estimates for risk premia are likely lower bounds, since portfolio restrictions would raise them.

[9] Asset premia depend on the stochastic structure of the economy, which is time invariant under a first-order solution. Hence, I can only evaluate average premia over the estimation periods. In a counterfactual exercise, I reestimate the model for two different periods to study how changes in the volatility and persistence of shocks affect premia.

the premium reflects both the asset sensitivity and the degree of risk sharing.[10]

This reflects the standard consumption-based asset pricing logic: risk premia arise when asset returns covary negatively with marginal utility. Assets that deliver low returns in states where marginal utility is high must offer a premium as compensation for poor consumption insurance. Since λ_z depends on the distribution of marginal utility responses across households, risk premia are also shaped by the heterogeneity of aggregate risk exposures.

Finally, since the risk premium is additively separable across shocks, I can compute the contribution of each shock z to an asset's total premium as

$$\Omega_{k,z} = \frac{X_{zk}\lambda_z\overline{\sigma}_z^2}{b^k}. \tag{10}$$

This decomposition makes it possible to identify which shocks drive asset premia.

In summary, the approach provides a tractable and powerful way to compute endogenous portfolio allocations and risk premia in heterogeneous-agent models using only first-order impulse responses and static model primitives, without solving the model to second order.

2.3 New Keynesian Firm Sector

We assume a three-tier production structure with a representative wholesale producer, a continuum of retailers, and a final goods producer. The wholesale producer creates a homogeneous wholesale good that retailers differentiate into specific varieties. The final goods producer bundles differentiated varieties into the final good. The wholesale firm accumulates capital subject to investment adjustment costs, while retailers set the prices of their product subject to a Calvo (1983) adjustment friction.

Final goods firm: The final goods firm bundles all j varieties using a Dixit-Stiglitz aggregator

$$Y_t = \left(\int_0^1 Y_{jt}^{\frac{1}{\mu_t^p}} dj \right)^{\mu_t^p} \tag{11}$$

[10] Note that (9) computes asset premia from the compensation households require for bearing aggregate risk. Unlike global solution methods, this approach does not necessarily reproduce the time-series properties of prices and payoffs in a fully nonlinear economy. Auclert et al. (2024) demonstrates that the method delivers identical portfolio holdings when replicating the models of Krusell and Smith (1997) and Bhandari et al. (2023). Using the same approach, it is also possible to reproduce the asset premia reported by Krusell and Smith (1997), confirming that the methodology successfully matches the premia implied by models solved with global solution techniques.

with elasticity of substitution between varieties of $\mu_t^p/(\mu_t^p - 1) > 1$. We assume that μ_t^p follows a log-AR(1) process with persistence ρ_p and shocks $\epsilon_t^p \sim N(0, \sigma_p^2)$ around the mean of the steady state price markup μ_p. Cost minimization of the final goods producer yields demand Y_{jt} for the individual variety j as

$$Y_{jt} = \left(\frac{P_{jt}}{P_t}\right)^{-\mu_t^p/(\mu_t^p-1)} Y_t, \tag{12}$$

where P_{jt} is the price of the individual variety j is offered at and $P_t = \int_0^1 \left(P_{jt}^{\frac{1}{1-\mu_t^p}} dj\right)^{1-\mu_t^p}$ denotes the aggregate price level.

Retail firms: There exists a unit interval of j monopolistically competitive retail firms. Each retail firm buys a homogeneous wholesale good from the wholesale firm at the price mc_t and costlessly differentiates the good into a variety j, for which the producer is a monopolist. As a result of monopolistic competition, each retailer generates a profit which it distributes to equity holders. Each retail firm sets the price for the variety P_{jt}, subject to a Calvo (1983) adjustment-friction with price indexation. Retailers that are unable to re-optimize during the period adjust their price according to the following indexation rule:

$$P_{jt} = P_{jt-1}\Pi_{t-1}^{\iota_p}\Pi^{1-\iota_p}, \tag{13}$$

where Π is steady state inflation, and ι_p reflects the degree of indexation to lagged aggregate inflation Π_{t-1}. Retail firms that can re-optimize, choose a new reset price P_{jt}^* to maximize expected discounted profits until the next re-optimization given by

$$\mathbb{E}_t \sum_{s=0}^{\infty} \lambda_p^s \bar{\beta}^s \left(\frac{P_{jt}^* \Gamma_{t,t+s}}{P_{t+s}} - mc_{t+s}\right) Y_{jt+s} \tag{14}$$

subject to demand by the final goods producer (12) and $\Gamma_{t,t+s} = \prod_{k=1}^{s} \Pi_{t+s-1}^{\iota_p}\Pi^{1-\iota_p}$. λ_p denotes the probability not to adjust the price in a given period, and $\bar{\beta}$ denotes the average discount factor of households.[11] The corresponding first-order condition for price setting implies a Phillips curve,

$$\log(\Pi_t) = \frac{\bar{\beta}}{1+\bar{\beta}\iota_p}\mathbb{E}_t \log(\Pi_{t+1}) + \frac{\iota_p}{1+\bar{\beta}\iota_p}\log(\Pi_{t-1}) + \kappa_p\left(mc_t - \frac{1}{\mu^p}\right) + \mu_t^p, \tag{15}$$

[11] I need to make an assumption about the discount rate with which firms discount future events. Here, I follow Auclert, Rognlie and Straub (2025) and choose the average discount factor in the economy. The average discount factor is the value of the discount factors of households multiplied by the stationary distribution of the Markov Chain that determines the idiosyncratic fluctuations in β_{it}.

where the slope of the Phillips curve is given by $\kappa_p = \frac{1-\lambda_p\bar{\beta}}{1+\iota_p\bar{\beta}}\frac{1-\lambda_p}{\lambda_p}$. I assume a symmetric equilibrium in which aggregate profits in the economy are $d_t = (1 - \frac{1}{\mu_t})Y_t$. These profits are distributed to the owners of shares in the retail firms, which trade at a price q_t.

Wholesale firm: Wholesale goods are produced by a representative wholesale firm using labor and capital:

$$Y_t = Z_t K_{t-1}^{\alpha} N_t^{1-\alpha}, \tag{16}$$

where α is the capital share in production, Z_t is total factor productivity that follows a log AR(1) process with persistence ρ_Z and shocks $\epsilon_t^Z \sim N(0, \sigma_Z^2)$, N_t is the labor hired, and K_{t-1} is the capital stock owned by the wholesale firm. Capital accumulates within the firm subject to investment adjustment costs, so that for each unit invested, a firm has to pay the adjustment cost.

$$S\left(\frac{I_t}{I_{t-1}}\right) = \frac{1}{2\chi}\left(\frac{I_t}{I_{t-1}} - 1\right)^2, \tag{17}$$

where $1/\chi$ is the curvature of the function. Moreover, I allow for shocks to the marginal productivity of investment Ψ_t, such that the capital accumulation equation for the wholesale firm is

$$K_t = (1-\delta)K_{t-1} + \Psi_t\left[1 - S\left(\frac{I_t}{I_{t-1}}\right)\right] I_t, \tag{18}$$

where δ is the depreciation rate of capital. I assume that Ψ_t follows a log AR(1) process with persistence ρ_I and shocks $\epsilon_t^I \sim N(0, \sigma_I^2)$. The wholesale firm is perfectly competitive and takes the real wholesale price mc_t and real wage w_t as given, selling all output. In this setting, the wholesale firm entering period t with capital K_{t-1} and past investment I_{t-1} chooses the amount of labor N_t, capital K_t, and investment I_t to maximize its value:

$$J_t(K_{t-1}, I_{t-1}) = \max_{K_t, I_t, N_t} mc_t F(K_{t-1}, N_t) - w_t N_t - I_t + \mathbb{E}_t\left[\frac{1}{1+r_{t+1}} J_{t+1}(K_t, I_t)\right] \tag{19}$$

subject to the capital accumulation equation (18). $1 + r_t$ is the gross real interest rate on assets. The optimization problem implies the standard first-order condition for labor demand $w_t = (1-\alpha)mc_t Z_t\left(\frac{K_{t-1}}{N_t}\right)^{\alpha}$, as well as the expression for Tobin's Q and the firm's

investment decision:

$$Q_t = \mathbb{E}_t \left[\frac{1}{1+r_{t+1}} \left((1-\delta) Q_{t+1} + \alpha MC_{t+1} Z_{t+1} \left(\frac{K_t}{N_{t+1}} \right)^{\alpha-1} \right) \right] \tag{20}$$

$$1 = \Psi_t Q_t \left[1 - S\left(\frac{I_t}{I_{t-1}} \right) - S'\left(\frac{I_t}{I_{t-1}} \right) \frac{I_t}{I_{t-1}} \right] + \mathbb{E}_t \left[\frac{\Psi_{t+1} Q_{t+1}}{1+r_{t+1}} S'\left(\frac{I_{t+1}}{I_t} \right) \left(\frac{I_{t+1}}{I_t} \right)^2 \right] \tag{21}$$

Unions: Nominal wages are assumed to be sticky. As in Erceg, Henderson and Levin (2000), unions set nominal wages to maximize agent utility subject to adjustment costs. I adopt the microfoundations for nominal wage rigidities of staggered pricing as in Calvo (1983). I assume that unions that cannot optimally adjust their prices follow an indexation rule. Finally, I specify the disutility of labor as $v(n_{it}) = \varsigma \frac{n_{it}^{1+\frac{1}{\phi}}}{1+\frac{1}{\phi}}$. I assume that unions allocate all labor hours uniformly across agents, so that $n_{it} = N_t$. This leads to the wage Phillips curve:

$$\begin{aligned} \log(\Pi_t^w) = \frac{\bar{\beta}}{1+\bar{\beta}\iota_w} \mathbb{E}_t \log(\Pi_{t+1}^w) + \frac{\iota_w}{1+\bar{\beta}\iota_w} \log(\Pi_{t-1}^w) \\ + \kappa_w \left(\varsigma N_t^{\frac{1}{\phi}} - \frac{(1-\tau) w_t \int_0^1 e_{it} c_{it}^{-1/\sigma} di}{\mu^w} \right) + \mu_t^w, \end{aligned} \tag{22}$$

describing the dynamics of log-wage inflation Π_t^w as a function of aggregate hours N_t, aggregate posttax labor income $(1-\tau)w_t$, and the effective consumption aggregator $\int_0^1 e_{it} c_{it}^{-1/\sigma} di$ that measures how the consumption distribution affects the wealth effect on labor supply. μ_t^w follows a log-AR(1) process with coefficient ρ_w and shocks $\epsilon_t^w \sim N(0, \sigma_w^2)$ and the slope of the wage Phillips curve is given by $\kappa_w = \frac{1-\lambda_w\bar{\beta}}{1+\iota_w\bar{\beta}} \frac{1-\lambda_w}{\lambda_w}$.

2.4 Government Sector

The government sector consists of a fiscal authority and a monetary authority.

Fiscal Authority: Fiscal policy sets a tax rate τ_t on labor, spends G_t on goods, and issues non-contingent debt B_t, with an average return R_{t-1}^F. Since the overall tax revenue is $\tau_t w_t N_t$, the government budget constraint is given by

$$B_t = R_{t-1}^F B_{t-1} + G_t - \tau_t w_t N_t \tag{23}$$

We assume that fiscal policy is specified in terms of plans for government spending G_t which follows a log-AR(1) process with persistence ρ_G and shocks $\epsilon_t^G \sim N(0, \sigma_G^2)$ and a

tax rule:

$$\frac{\tau_t}{\tau^{ss}} = \left(\frac{\tau_{t-1}}{\tau^{ss}}\right)^{\rho_\tau} \left(\frac{B_{t-1}}{B_{t-2}}\right)^{(1-\rho_\tau)\gamma_\tau^B} \left(\frac{Y_t}{Y_{t-1}}\right)^{(1-\rho_\tau)\gamma_\tau^Y}, \tag{24}$$

where ρ_τ denotes the persistence of the tax rate, γ_τ^B denotes the elasticity of the tax rate to lagged debt growth, and γ_τ^Y denotes the elasticity of the tax rate to output growth. Given a real interest rate, the tax rule and the government budget constraint imply a process for bonds B_t.

Bond Maturity Structure: I model government debt instruments with a range of maturities. To incorporate different maturities in a tractable fashion, I follow Bayer, Born and Luetticke (2022) and assume that along all maturities the bonds are zero-coupon bonds with geometrical decay.[12] The bonds are priced recursively, and their ex-post returns contribute to the weighted average fiscal interest rate R_{t-1}^F the government has to pay to households.

Let q_t^n denote the price of a government bond at time t with maturity n and R_{t-1}^n denote the ex-post return of a bond. A no-arbitrage condition sets the price of each bond, and the ex-post return by definition:

$$q_t^n = \frac{(1-\delta^n)q_{t+1}^n + 1}{1 + r_{t+1}}, \quad \text{and} \quad R_{t-1}^n = \frac{(1-\delta^n)q_t^n + 1}{q_{t-1}^n} \quad \forall n \tag{25}$$

δ^n denotes the maturity-specific retirement rate of the bond and r_t is the risk-free real interest rate. The government pays the weighted average of the ex-post returns R_{t-1}^F across maturities:

$$R_{t-1}^F = \sum_n \omega_t^n \cdot R_t^n \quad \text{with} \quad \sum_n \omega_t^n = 1 \tag{26}$$

where ω_t^n denotes the share of government debt issued with maturity n at time t. This composite rate captures the average cost of servicing outstanding government debt, accounting for the composition of the debt portfolio.

Monetary Policy: Monetary policy sets the nominal interest rate i_t, using the following Taylor rule:

$$1 + i_t = (1 + i_{t-1})^{\rho_r} \Pi_t^{(1-\rho_r)\phi_\pi} \left(\frac{Y_t}{Y_{t-1}}\right)^{(1-\rho_r)\phi_Y} \exp(\epsilon_t^r) \tag{27}$$

[12] This assumption makes the price and the ex-post return of long-term bonds more exposed to more persistent shocks. This feature helps to match the empirical fact that the price of long-run bonds fluctuates more in response to shocks as either their cash-flows or their discount rates are affected by the shock.

where ρ_r denotes the persistence of the monetary policy rule, ϕ_π and ϕ_Y denote the elasticities of the nominal interest rate to inflation and output growth, and $\epsilon_t^r \sim N(0, \sigma_r^2)$ is an iid monetary policy innovation. Finally, I define the ex-ante real interest rate as $1 + r_t = (1 + i_t)/\Pi_{t+1}$ according to a Fisher equation.

2.5 Market clearing

In equilibrium, the goods market, the labor market, and the asset market have to clear:

$$Y_t = \int c_{it} di + I_t + G_t \qquad \int_0^1 n_{it} dj = N_t \qquad \int a_{it} di = B_t + q_t^{eq} + q_t K_t. \tag{28}$$

Where asset market clearing implies that the total savings of households have to be equal to total government debt B_t, the value of the equity market q_t^{eq}, and the value of the capital stock $q_t K_t$. I do not repeat market-clearing for each equity or for each asset, as I ensure these markets clear when computing the value of the equity index and when determining households' portfolios. I assume that all firms are symmetric such that $Y_{jt} = Y_t$, $d_{jt} = d_t$, $w_{jt} = w_t$, and $d_{jt} = d_t$.

3 Calibration and Estimation of the Model

This section describes the calibration of the steady-state and the subsequent estimation of the model using U.S. time-series data. The calibration ensures that the model reproduces the levels of key endogenous variables, while the estimation targets their dynamic behavior. First, I calibrate the steady state so that the model matches key dimensions of household heterogeneity and the time series averages of aggregate variables. I then present the Bayesian estimation on U.S. data, discuss the resulting parameter estimates and model fit, and assess the validity of the estimated dynamics.

3.1 Calibration of the Steady State

Table 1 presents the calibration parameters. The parameter choices of the household side largely follow Auclert, Rognlie and Straub (2025). To start with, the exogenous income process is the discretized permanent-transitory income process of Kaplan, Moll and Violante (2018), based on their estimates from the Social Security Administration data. I assume both the standard intertemporal elasticities of substitution, ρ, and the Frisch elasticity of labor supply, ϕ, equal one, and calibrate the disutility from labor ς to normalize labor supply N_t to unity. Moreover, I set the risk-aversion parameter equal to

Table 1 Calibration Details (Quarterly Frequency)

Parameter	Value	Description	Source / Target
Preferences			
ρ	1.000	Elasticity of intertemporal sub.	Standard value
γ	6.000	Risk aversion	Guvenen (2009)
ς	0.787	Disutility from labor	Labor normalization
ϕ	1.000	Frisch elasticity of labor	Standard value
Idiosyncratic risk			
β^H	0.996	Discount factor patient HHs	Assets-to-Output: 18.0
Δ^β	0.010	Difference in discount factors	Aggregate MPC: 0.1
ω	0.635	Fraction of patient HHs	U.S. Lorenz Curve of wealth
ϖ	0.010	Prob. to change patience	Krusell and Smith (1997)
Firms			
Z	0.501	Steady state productivity	Output Normalization
α	0.286	Capital income share	Capital-to-Output: 11.9
δ	0.018	Capital depreciation	Historical Average from NIPA
μ^p	1.020	Price Markup	Equity-Price-to-Output: 3.8
μ^w	1.000	Wage Markup	No transfers in steady state
Government			
G	0.211	Government expenditure	Expenditure-to-Output: 0.21
B	1.700	Government debt	Debt-to-Output-Ratio: 1.7
r	1.000	Real interest rate in (%)	Postwar quarterly average
τ	0.309	Tax rate	Finances debt and expenditure

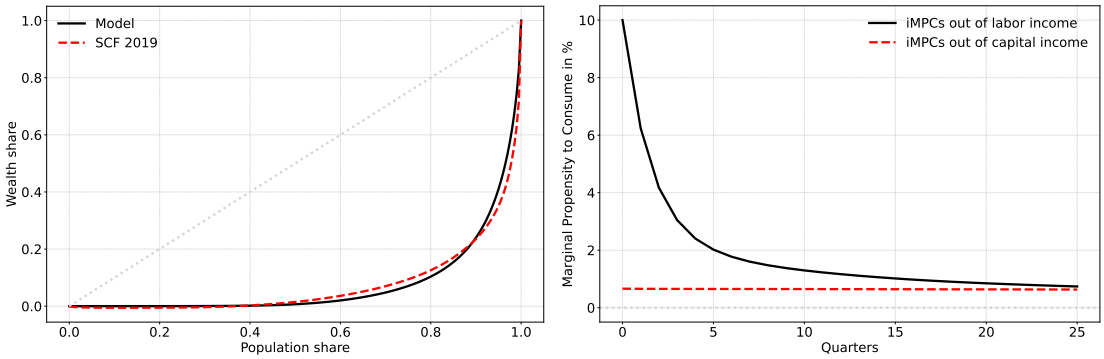
Notes: All parameters in the table are calibrated to a quarterly frequency. Probabilities represent the probability within a single quarterly period. Interest rates are reported as quarterly rates.

6 as in Guvenen (2009). This parameter value lies between the commonly used value of 10 in the finance literature (for example, Bansal and Yaron, 2004) and the value of 1 used with CRRA preferences in macro models (for example, Krusell and Smith, 1997).

Next, I calibrate the heterogeneity in discount factors to match key moments from U.S. household microdata. I jointly choose the patient discount factor β^H, the gap Δ^β between patient and impatient types, and the stationary share of patient households ω to match aggregate assets, to target an aggregate marginal propensity to consume out of labor income of 0.10 per quarter, and to minimize the distance between the model implied wealth Lorenz curve and its U.S. counterpart.[13] The probability of a patience

[13] I target a lower quarterly MPC than Auclert, Rognlie and Straub (2024), since Orchard, Ramey and Wieland (2025) provide recent evidence that MPC estimates for nondurable consumption are below 0.2 per quarter.

Figure 1 Fit of wealth inequality and aggregate marginal propensities to consume



Notes: The left panel illustrates the fit of the model-implied Lorenz for household wealth compared to the Lorenz curve estimated from the SCF in 2019 by Auclert, Rognlie and Straub (2025). The right panel illustrates the model's intertemporal marginal propensities to consume (iMPCs) out of labor and capital income.

redraw ϖ follows Krusell and Smith (1997) by matching the arrival of a new generation every 25 years.

The left panel of figure 1 compares the model-implied Lorenz curve with the empirical curve from the 2019 Survey of Consumer Finances. The overall fit is close, but the model understates wealth concentration at the top, as is common in models without capital income heterogeneity (see Stachurski and Toda, 2019). The right panel of figure 1 plots the model's aggregate intertemporal marginal propensities to consume (iMPC). While I target an impact MPC out of labor income of 0.10, all other MPCs are untargeted. In line with microdata estimates such as Fagereng, Holm and Natvik (2021), the model's iMPCs are large on impact and then decline quickly. The untargeted MPC out of capital income is 0.01, which lies at the lower end of the empirical range 0 to 0.05 reported by Chodorow-Reich, Nenov and Simsek (2021).

I set the values of the firm and government sector to match time-series averages from U.S. national accounts. I provide a detailed description of the data used and the calculations in Appendix III. First, I set TFP Z_t so that output is normalized to one. I set α to target a quarterly capital-to-output ratio of 11.9 with a depreciation rate of $\delta = 1.775$ percent, consistent with time-series averages for the periods considered. The markup μ^p is chosen to generate a quarterly stock market-to-GDP ratio of $q_t/Y_t = 3.9$, consistent with historical averages. I assume that the wage markup μ^w equals unity, such that there are no union transfers in the steady state. I set government expenditure equal to 21.1% of GDP and total government debt equal to 1.7 times quarterly GDP, corresponding to an annual debt-to-GDP ratio of 42.5%, both reflecting historical averages. The quarterly

Table 2 Calibration of the public debt structure

Bond Label	Maturity Tranche n	Share $\omega^{(n)}$ of Total Debt	Duration $1/\delta^{(n)}$ in Quarters
3M	$\leq 3M$	0.154	1.00
6M	$6M - 9M$	0.129	2.31
1Y	$1Y$	0.043	4.00
2Y	$2Y$	0.138	8.00
5Y	$3Y - 7Y$	0.296	18.32
10Y	$8Y - 12Y$	0.095	37.36
20Y	$15Y \leq$	0.145	95.74

Notes: Maturities show the maturity of the zero-coupon bonds in months (M) or years (Y). Share in total debt $\omega^{(n)}$ represents the fraction of total government debt with the respective maturity. The duration $\delta^{(n)}$ shows the average duration in quarters across the neighboring maturities I clustered into the seven subgroups.

risk-free real interest rate is set at 1.0%, in line with the U.S. postwar average. The labor tax rate τ is set to 0.309 to balance the government's budget constraint.

To calibrate the maturity structure of government debt, I use historical averages from the database of De Graeve and Mazzolini (2023), which reports debt values at constant maturities for many OECD countries. First, I calculate the average market value of public debt for each maturity in the dataset. I then combine neighboring maturities to obtain seven groups that approximately represent three months, six months, one year, two years, five years, ten years, and twenty years. I chose the tranches to obtain approximately equal weights and to cover key maturities along the yield curve. As data on duration by maturity is unavailable, I assume that all debt in the dataset consists of zero-coupon bonds. For each group m, I set the duration parameter δ^m equal to the weighted average maturity of its empirical counterpart. I then label each of these groups according to a whole month or year.[14] Table 2 reports the resulting calibration parameters for the debt share and the duration. 32.7% of government debt has a maturity equal to or below one year, 43.4% has a maturity between one year and five years, and 24% has a maturity longer than five years.

[14] I label the final tranche as 20-year bonds even though its average duration is closer to 25 years. The label indicates that most securities in this tranche have a 20-year maturity and that reliable yield data are available at that horizon. The longer average duration arises from a small share of bonds with maturities of more than 30 years.

3.2 Bayesian Estimation of the Model

After calibrating the model's steady state, I use Bayesian estimation to match the time-series dynamics of U.S. macroeconomic aggregates. For the estimation, I use a macroeconomic time series similar to that of Bayer, Born and Luetticke (2024), covering the period from the third quarter of 1954 to the fourth quarter of 2019. I augment this dataset with updated series from Shiller (1989) on equity prices, dividends, and returns. The combined dataset includes growth rates of real GDP, consumption, investment, and wages. Hours worked, the (shadow) federal funds rate, the inflation rate, and real equity returns are expressed in logarithmic levels.[15] A detailed description of the data sources and the transformations applied is provided in Appendix III. Note that among all asset returns, I include only the federal funds rate and the equity return as observables in the estimation. As a result, the estimation does not discipline model-implied asset premia, so comparing them with their empirical counterparts provides out-of-sample validation of the model.

To estimate the model, I first solve for its equilibrium dynamics using the sequence space approach of Auclert et al. (2021). I then employ the Differential Independence Mixture Ensemble (DIME) sampler of Boehl (2024) to characterize the posterior density of the model's parameters. DIME combines differential evolution with independence sampling and runs an ensemble of jointly evolving local and global chains. The local kernel explores the neighborhood of a given chain, while the global kernel reshuffles states across the current posterior support. This design shortens the burn-in phase and enables efficient sampling, so DIME does not require prior mode optimization. Instead, the sampler learns the posterior's shape from the draws themselves, thereby increasing robustness to misspecified priors. For the estimation, I use 128 parallel global chains that run for 10,000 iterations. I discard the first 5,000 iterations as burn-in. Columns 1-4 of table 3 illustrate the parameters I estimate, their assumed prior distributions and their posteriors.

Priors Column 3 in table 3 illustrates the priors I use for the estimation. The priors on the stochastic processes are harmonized as much as possible.[16] Innovation standard deviations follow Inverse Gamma distributions with mean 0.1 and standard deviation 0.25. Autoregressive coefficients follow Beta distributions with mean 0.5 and standard

[15] Following Bayer, Born and Luetticke (2024), I use the shadow federal funds rate constructed by Wu and Xia (2016) during periods when the zero lower bound constrains the federal funds rate.

[16] One might expect a higher prior for the standard deviation of the asset price shock, since equity returns are the most volatile observable. Robustness checks show that increasing the prior mean for this shock leaves the results unchanged.

Table 3 Bayesian estimation results: shock and policy parameters

		Prior		Posterior			
Shock Parameter	**Distribution**	**Mean**	**SD**	**Mean**	**Median**	**5%**	**95%**
$\sigma_q \cdot 100$	Inv. Gamma	10.0	25.0	0.420	0.420	0.325	0.543
ρ_q	Beta	0.5	0.2	0.985	0.984	0.978	0.990
$\sigma_\zeta \cdot 100$	Inv. Gamma	10.0	25.0	0.316	0.316	0.266	0.375
ρ_ζ	Beta	0.5	0.2	0.047	0.053	0.009	0.152
$\sigma_z \cdot 100$	Inv. Gamma	10.0	25.0	0.674	0.673	0.615	0.739
ρ_z	Beta	0.5	0.2	0.933	0.932	0.898	0.959
$\sigma_I \cdot 100$	Inv. Gamma	10.0	25.0	2.534	2.533	2.248	2.862
ρ_I	Beta	0.5	0.2	0.956	0.956	0.938	0.969
$\sigma_p \cdot 100$	Inv. Gamma	10.0	25.0	0.242	0.242	0.219	0.268
ρ_p	Beta	0.5	0.2	0.941	0.940	0.902	0.965
$\sigma_w \cdot 100$	Inv. Gamma	10.0	25.0	1.508	1.505	1.205	1.904
ρ_w	Beta	0.5	0.2	0.932	0.932	0.904	0.953
$\sigma_G \cdot 100$	Inv. Gamma	10.0	25.0	1.651	1.651	1.519	1.798
ρ_G	Beta	0.5	0.2	0.970	0.970	0.955	0.981
$\sigma_r \cdot 100$	Inv. Gamma	10.0	25.0	0.262	0.262	0.232	0.296

		Prior		Posterior			
Policy Parameter	**Distribution**	**Mean**	**SD**	**Mean**	**Median**	**5%**	**95%**
ρ_r	Beta	0.5	0.2	0.748	0.748	0.707	0.787
ϕ_π	Gamma	1.5	0.3	1.691	1.689	1.595	1.802
ϕ_Y	Normal	0.1	0.1	0.167	0.167	0.101	0.233
ρ_τ	Beta	0.5	0.2	0.255	0.255	0.042	0.733
γ_τ^B	Normal	0.0	1.0	1.022	0.993	0.164	1.980
γ_τ^Y	Normal	0.0	1.0	0.286	0.261	-0.830	1.498
λ_p	Beta	0.5	0.1	0.499	0.499	0.325	0.672
λ_w	Beta	0.5	0.1	0.430	0.430	0.368	0.494
ι_p	Beta	0.5	0.2	0.499	0.499	0.229	0.771
ι_w	Beta	0.5	0.2	0.072	0.074	0.027	0.160
χ	Gamma	4.0	2.0	2.539	2.701	0.825	6.349

Notes: Posterior estimates are based on Bayesian inference using the DIME sampler by Boehl (2024). The sampler was run with 128 parallel chains for 10,000 iterations each. I discard the first 5,000 iterations as burn-in. Reported values are posterior means, medians, and 90 percent credible intervals. Shock standard deviations are scaled by 100 to enhance readability.

deviation 0.2. This choice is weakly informative, keeps probability mass away from the boundaries, and treats the shocks symmetrically.

For policy parameters, the priors follow Bayer, Born and Luetticke (2024), which aligns the Taylor rule and interest rate inertia with standard New Keynesian benchmarks.

The inflation coefficient ϕ_π has a Gamma prior with mean 1.5 and standard deviation 0.3. The output coefficient ϕ_Y has a Normal prior with mean 0.1 and standard deviation 0.1. Interest rate smoothing and tax rate smoothing, ρ_r and ρ_τ, have Beta priors with mean 0.5 and standard deviation 0.2. The feedback of debt and output growth in the tax rule, γ_τ^B and γ_τ^Y, follows standard Normal priors.

For price and wage stickiness, λ_p and λ_w, and for indexation, ι_p and ι_w, I adopt priors in the spirit of Smets and Wouters (2007). The stickiness parameters have Beta priors with mean 0.5 and standard deviation 0.1. The indexation parameters have Beta priors with mean 0.5 and standard deviation 0.2. Finally, following Justiniano, Primiceri and Tambalotti (2011), the investment adjustment cost parameter χ has a Gamma prior with mean 4.0 and standard deviation 2.0. Overall, the prior block is comparable to the main references and diffuse enough to let the data discipline the posterior.

Posterior estimates Column 4 in table 3 illustrates the mean, median, as well as the 5 and 95 percentiles of the posterior distribution. Checks on the convergence of the estimator are reported in Appendix IV.

The estimated shock processes are persistent, while the preference shock is the exception, with little persistence ($\rho_\zeta \approx 0.047$). Moreover, innovation scales are heterogeneous. Investment and fiscal innovations have the largest standard deviations, followed by wage innovations. In general, these magnitudes and persistence patterns are broadly in line with medium-scale New Keynesian estimates that feature persistent real and fiscal drivers together with comparatively lower price-setting volatility.

The estimates of the monetary policy rules are consistent with previous estimates. The posterior mean for interest rate smoothing is $\rho_r \approx 0.748$, which lies between 0.6 and 0.8, as reported in benchmark studies. The inflation coefficient is $\phi_\pi \approx 1.691$ and well within typical post-1990 estimates. The output coefficient is $\phi_Y \approx 0.167$, which sits in the standard range between 0.1 and 0.3. The fiscal block indicates modest persistence in the tax rule with $\rho_\tau \approx 0.255$, a positive feedback of debt with $\gamma_\tau^B \approx 1.022$, and a smaller feedback of activity with $\gamma_\tau^Y \approx 0.286$.

Nominal rigidities are moderate. The posterior implies price stickiness $\lambda_p \approx 0.499$ and wage stickiness $\lambda_w \approx 0.430$, which point to meaningful real rigidity with somewhat more frequent wage adjustment than price adjustment. Indexation is asymmetric. Price indexation is moderate with $\iota_p \approx 0.499$, whereas wage indexation is low with $\iota_w \approx 0.072$. Relative to standard medium-scale estimates, these values fall within familiar ranges and suggest that backward-looking behavior is more important in prices than in wages in this sample.

Table 4 Annualized Asset Premia in Excess of the 3-month Government Bond Return

Asset	**Data** (%)	**HA** (%)	**RA** (%)
Equity	5.01	4.92	0.00074
Bond 6m	0.19	0.07	0.00007
Bond 1y	0.36	0.24	0.00009
Bond 2y	0.72	0.64	0.00014
Bond 5y	1.29	1.26	0.00022
Bond 10y	1.77	1.71	0.00026
Bond 20y	2.18	2.01	0.00028

Notes: Annualized asset premia for the estimated heterogeneous-agent model, a representative-agent variant, and their empirical counterparts. The empirical equity premium is calculated as the sample mean of annualized stock excess returns over a long-term bond, proxied by the return on a ten-year zero-coupon bond. Empirical term premia are calculated as the excess returns on zero-coupon bonds at constant maturities relative to the three-month zero-coupon bond. The empirical equity return series is identical to the series used in the estimation. Zero-coupon yields are from the Board of Governors of the Federal Reserve System. Premia are computed following Auclert et al. (2024): $\frac{R_1 - R_0}{R} \approx -X\,\bar{\lambda}\,\sigma^2$, where X is the ex-post variation of an asset's excess return over the three-month bond return and $\bar{\lambda}$ is the aggregate pricing kernel.

4 The Distributional Origins of Asset Premia

This section uses the estimated model to analyze U.S. asset premia. First, I show that the model replicates the untargeted level of premia observed over the estimation period. Thereafter, I decompose these premia into contributions from individual structural shocks and explain their magnitudes by tracing how aggregate risk is distributed across households.

4.1 Decomposing U.S. Asset Premia

While the model is estimated to match the dynamics of equity returns and the federal funds rate, it is not obvious that it can also reproduce the observed levels of asset premia. Table 4 shows that it does. It reports annualized premia in percentage points over the three-month government bond for both the heterogeneous-agent (HA) model and a representative-agent (RA) version. The HA model generates sizable premia that are close to the time series averages over the estimation period. It produces an annualized equity premium of 4.92 percentage points, which is close to the average empirical equity premium of 5.01 percentage points. It also matches the slope of the yield curve and delivers term premia of 1.26, 1.71, and 2.01 percentage points for five, ten, and twenty

Table 5 Decomposition of the Annualized Asset Premia into Risk Components

	Equity Premium		1Y Term Premium		10Y Term Premium	
Risk Component	Abs.	Rel. (in %)	Abs.	Rel. (in %)	Abs.	Rel. (in %)
Asset Price	2.21	44.86	-0.01	-5.56	-0.11	-6.46
Discount-Factor	-0.02	-0.44	-0.01	-5.61	-0.02	-1.15
Monetary Policy	0.25	5.13	0.16	65.37	0.21	12.09
Government Exp.	0.43	8.74	0.01	2.61	0.05	2.96
Productivity	0.62	12.65	0.04	17.86	0.13	7.60
Inv. spec. Prod.	0.82	16.63	0.05	20.22	1.36	79.93
Price Markup	-0.10	-1.97	0.00	1.92	-0.01	-0.39
Wage Markup	0.71	14.41	0.01	3.18	0.09	5.43
Total	4.92		0.24		1.71	

Notes: Contribution of aggregate shocks to the equity premium, 1-year term premium (1Y Term Premium), and the 10-year term premium (10Y Term Premium). The contribution is calculated according to equation (10), hence as the fraction of the total premium explained through one shock. For each premium, the first column shows the absolute contribution of the component, and the second column shows the risk component's relative contribution to the overall premium. Positive values indicate premia that households require to hold the asset, while negative values indicate return discounts that households accept.

years, respectively, compared with 1.29, 1.77, and 2.18 percentage points in the data.

Table 4 also allows for a comparison between the asset premia predicted by the heterogeneous agent (HA) model and its representative agent (RA) counterpart. The RA model shares all structural features of the HA model, including segmented financial markets, but assumes that households can perfectly insure against idiosyncratic income risk. I compute asset premia for the RA model using the identical methodology as in the HA model. While the HA model generates realistic asset premia, the RA model does not. This comparison highlights that imperfect insurance against idiosyncratic income risk, as in the HA model, is essential for generating realistic asset premia, even with recursive preferences and moderate risk aversion.

Overall, the model reproduces average asset premia well, which justifies using it as a laboratory to decompose premia in the next step. Table 5 reports a decomposition of the model-implied equity premium, the one-year term premium, and the ten-year term premium into contributions from eight structural shocks. For each premium, the first column shows the component's absolute contribution, and the second column reports its share of the total premium. A positive contribution indicates that households demand a premium for bearing the respective shock through the asset. In contrast, a negative contribution implies that the asset provides a hedge against that shock, leading households to price it at a discount.

For the equity premium, the asset price shock is the largest component, accounting for 2.21 percentage points, or 44.9 percent of the total. Hence, a considerable share of the equity premium reflects risk unrelated to fundamental shocks. Conventional business-cycle shocks explain the remaining portion. Supply-side shocks to aggregate productivity, investment-specific productivity, and the wage markup jointly account for 42 percent of the total. For the one-year term premium, the monetary policy shock is the dominant source, contributing 0.16 percentage points (65 percent), followed by productivity and investment-specific productivity shocks, each contributing 0.04 and 0.05 percentage points (18 and 20 percent, respectively). At the ten-year horizon, this pattern reverses: the investment-specific technology shock explains 1.36 percentage points (80 percent) of the premium, while monetary policy accounts for only 0.21 percentage points (12 percent). Overall, the model associates short-maturity term premia primarily with monetary policy shocks and long-maturity premia with persistent investment-specific technology shocks.[17]

4.2 Asset Premia and Aggregate Risk-Sharing

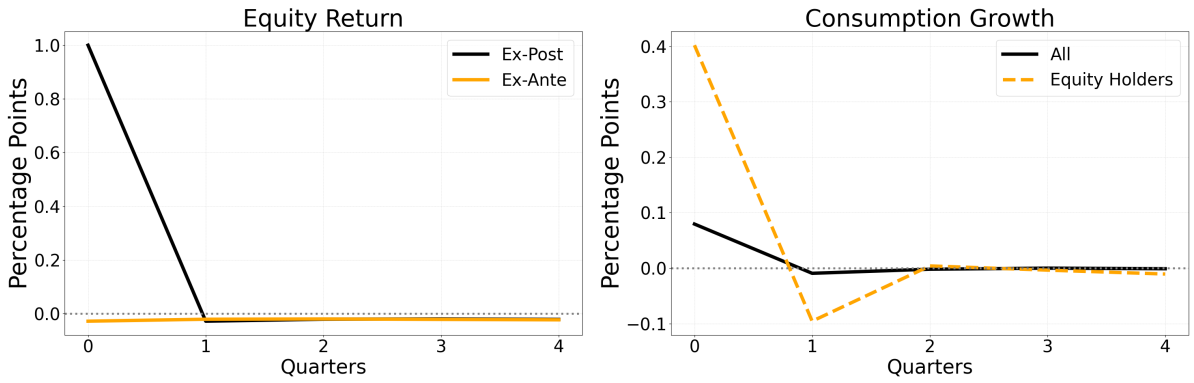
As highlighted before, the level of asset premia is determined by households' residual exposure to aggregate risk, which, in turn, depends on how aggregate shock exposure is distributed across households. When trading in the financial market leaves households with substantial residual fluctuations in marginal utility after aggregate shocks, they demand premia for holding the exposed assets.

To illustrate how differential exposure to aggregate shocks translates into premia, Figure 2 reports impulse responses to a normalized asset price shock that raises the equity price by one percent relative to the steady state. The left panel shows that the shock increases the ex-post equity return on impact, while higher prices today reduce expected future returns, lowering the ex ante return. The right panel illustrates the heterogeneous consumption responses across households. Consumption of equity holders rises by about 0.4 percentage points on impact, compared with less than 0.1 percentage points for aggregate consumption.

These consumption responses reflect how aggregate risk exposure is distributed across households after financial market trading. In the stationary distribution, many households hold little or no wealth and remain highly exposed to idiosyncratic income fluctuations. Because a price decline that coincides with an idiosyncratic drop in labor income generates significant utility losses, equity is costly to hold for low-wealth house-

[17] Appendix V illustrates the impulse response of the economy to an investment-specific technology shock.

Figure 2 Impulse Responses to a normalized Asset Price Shock



Notes: Impulse responses for the ex-post and ex ante equity return, aggregate consumption growth, and consumption growth of equity holders. The left panel reports changes in equity returns in percentage points. The right panel reports changes in the growth rates of the two consumption measures in percentage points. Responses are to a normalized asset price shock that raises the equity price by one percent relative to its steady state. The shock corresponds to roughly one quarter of its estimated standard deviation.

holds. Hence, the few households that ultimately hold equity are wealthy and well insured against idiosyncratic income fluctuations, with average wealth about 1.7 times the economy-wide mean. Despite this wealth, the residual risk of the asset price shock is concentrated among this group of equity holders. As shown in Figure 2, this residual exposure to equity risk induces large fluctuations in their consumption growth, about four times the aggregate average. The amplification of equity holders' consumption response relative to the average illustrates the magnitude of their residual risk and helps rationalize the size of the equity premium.

We can apply the same logic to rationalize the term premium. Unlike equity, a one-year bond is not subject to large revaluation effects due to its low duration. Its returns vary little, so low-wealth households tend to hold it because it provides consumption insurance with stable payoffs. Movements in one-year bond returns mainly reflect monetary policy, which has a limited direct impact on these households because their consumption is largely hand-to-mouth rather than set on the Euler margin. Together, these features imply low residual exposure of one-year bondholders to aggregate risk, which rationalizes the small one-year term premium.

In contrast to the one-year bond, the ten-year bond carries high duration, so its price is much more sensitive to shocks. By the same logic as above, this greater revaluation risk makes long-maturity bonds a poor hedge for low-wealth households, so they are concentrated in a few high-wealth portfolios. The owners, therefore, bear a larger

residual exposure to shocks that move long bonds, most notably the investment-specific productivity shock, whose persistence is transmitted through capital accumulation, production, and investment.[18] This pattern mirrors the equity logic and rationalizes an upward-sloping and sizable term premium.

5 Decomposing U.S. Business Cycles and Inequality

Having decomposed asset premia, I now return to study the drivers of U.S. business cycles and inequality. I focus on how the inclusion of the asset price shock changes these dynamics. To quantify its role, I compute conditional variance decompositions at business-cycle frequencies using the frequency-domain approach of Uhlig (2001).

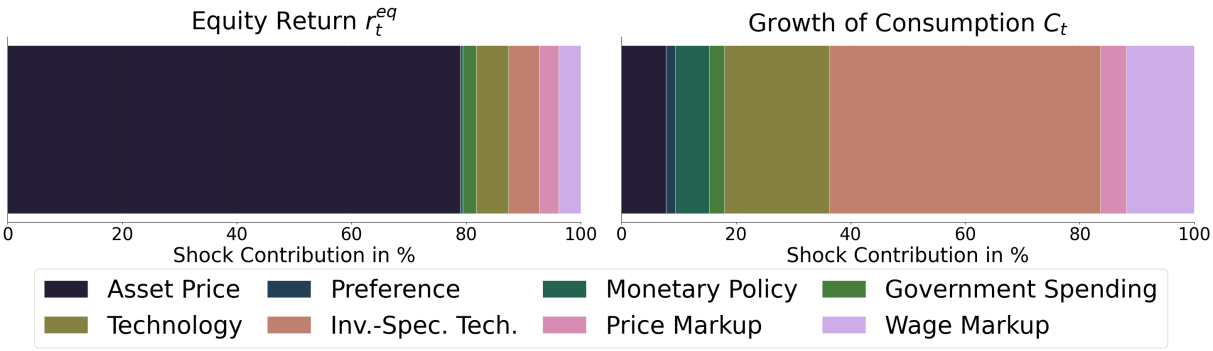
5.1 Decomposing U.S. Business Cycles

Figure 3 reports the conditional variance decomposition for equity returns and consumption growth. Appendix V illustrates the conditional variance decomposition for all aggregate variables. The left panel shows that the asset price shock explains 79 percent of the variation in equity returns. The remaining 21 percent is mainly driven by investment-specific technology, aggregate technology, and markup shocks. This confirms that most business-cycle variation in equity returns originates not from fundamental shocks but from sources captured by the asset price shock. While the asset price shock dominates the equity return, the right panel shows that it explains only 7.8 percent of the variance in aggregate consumption growth. Consumption dynamics are instead driven primarily by supply-side forces: investment-specific technology accounts for 47.3 percent of the variance, followed by aggregate technology, wage, and price markup shocks, which together contribute another 34.7 percent. In contrast, demand-side shocks jointly explain only 10.2 percent of the variation in consumption growth.

It might be surprising that the shock that explains the largest fraction of equity returns accounts for only a small fraction of the variation in consumption growth. Through the lens of the structural model, it is possible to investigate the transmission mechanisms in detail. Intuitively, equity accounts for less than one quarter of households' total assets, so even large swings in the value of equity generate only modest aggregate wealth effects. In addition, equity holders have low marginal propensities to consume out of total wealth, so changes in equity payoffs translate into only modest changes in consumption.

[18] See Appendix V for the impulse response to an investment-specific productivity shock.

Figure 3 Conditional Variance Decomposition of Aggregate Variables



Notes: Conditional variance decompositions for equity returns and consumption growth were computed at business-cycle frequencies (forecast horizons of 6 to 32 quarters) using the estimated model. The coloured areas show the share of each variable's variance attributable to a given structural shock.

I can illustrate these channels formally through the decomposition of Auclert, Rognlie and Straub (2024).[19] Using their conceptual framework, up to first order, the change in the sequence of aggregate consumption can be written as the sum of three household-side components:

$$d\mathbf{C} \;=\; \mathbf{M}\cdot d\mathbf{Z} \;+\; \mathbf{M}^{r}\cdot d\mathbf{r} \;+\; \mathbf{m}^{cap}\, d\text{cap}_0, \tag{29}$$

The matrices $\mathbf{M}$ and $\mathbf{M}^r$ are Jacobians that capture, respectively, the marginal propensities to consume out of changes in the sequence of labor income $d\mathbf{Z}$ and the elasticities of aggregate consumption with respect to future real interest rates $d\mathbf{r}$. The vector $\mathbf{m}^{cap}$ is the marginal propensity to consume out of capital gains and measures how aggregate consumption changes when the value of assets changes by $d\text{cap}_0$.[20] More intuitively, $\mathbf{M}$ and $\mathbf{m}^{cap}$ quantify the strength of the income and the wealth effect coming from changes in the sequence of labor income and asset valuations. In contrast, $\mathbf{M}^r$ quantifies the strength of the substitution effect coming from changes in the interest rate. The change in the sequence of aggregate consumption is the sum of all of these effects.

The wealth effect from asset revaluation can be further decomposed into the contributions of individual assets.[21] When focusing on the isolated wealth effect of a change

[19] The following derivation builds on equations (34) and (35) in the main text, as well as the proof of Proposition 8 in the appendix of Auclert, Rognlie and Straub (2024). For a more detailed decomposition of wealth effects in heterogeneous-agent settings, see Gong (2025a), and for a general decomposition of transmission channels in HANK models, see Gong (2025b).

[20] Formally, the aggregate marginal propensity to consume (MPC) out of labor income is computed as $\mathbf{M} \equiv [\partial \mathcal{C}_t/\partial Z_s]_{ts}$, the elasticity of consumption with respect to the real interest rate is calculated as $\mathbf{M}^r \equiv [\partial \mathcal{C}_t/\partial \log(1+r_s)]_{ts}$, and, with slight abuse of notation, the MPC out of unexpected capital gains on asset k is calculated as $m_t^k \equiv \partial \mathcal{C}_t/\partial(p_0+d_0)$.

[21] With multiple assets, the revaluation term can be written as $d\text{cap}_0 = (1+r)\boldsymbol{\omega}\, A\, d\boldsymbol{r}^{post}$, where $\boldsymbol{\omega} = [q^k/A]_k$ denotes portfolio shares across assets k, and $d\boldsymbol{r}^{post}$ represents the vector of ex-post changes in

in the value of a single asset on consumption, this effect depends on the change in the valuation of the asset studied. The direct impact of an asset price shock on consumption through the revaluation of equity can then be expressed as

$$d\mathbf{C}^{val} = \mathbf{m}^{cap}(1+r)q^{eq}\frac{\partial r^{eq}}{\partial \epsilon^q}d\epsilon^q, \tag{30}$$

where $\mathbf{m}^{cap}$ denotes the MPC out of capital income, q^{eq} is the aggregate value of equity, and $\frac{\partial r^{eq}}{\partial \epsilon^q}d\epsilon^q$ denotes the impact impulse response (IRF) of the equity payoff to the asset price shock. The expression shows that aggregate consumption changes with the size of the valuation adjustment, weighted by households' propensity to consume out of an additional unit of wealth.

Given the calibrated parameters, it is possible to compute the direct effect. Assuming a one percent increase in asset prices (that is, $\frac{\partial r^{eq}}{\partial \epsilon^q}d\epsilon^q = 0.01$), an MPC out of capital income of one percent, and an equity value of $q^{eq} = 3.9$, the resulting consumption response is

$$d\mathbf{C}^{val} = 0.01 \times (1+r) \times 3.9 \times 0.01 \approx 0.04 \tag{31}$$

Hence, a one percent increase in equity prices raises aggregate consumption directly by only about 0.04 percent, indicating that the direct wealth effect from the asset price shock is quantitatively small. Even though such shocks can generate equity-return volatility of about ten percent per quarter, their impact on aggregate consumption volatility remains modest. Note that Chodorow-Reich, Nenov and Simsek (2021) estimates that a one-dollar increase in stock market wealth raises consumption by 3.23 cents. The model-based estimate obtained here is of a similar order of magnitude and complements their empirical findings from a structural perspective.

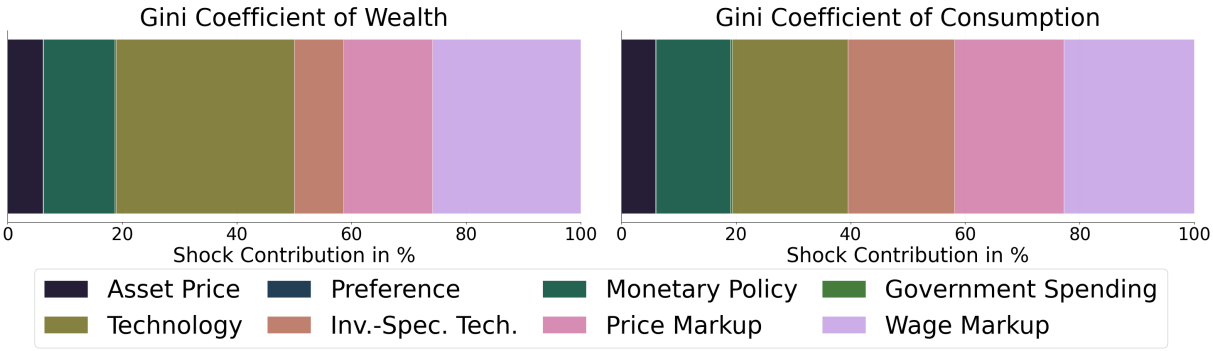
5.2 Decomposing U.S. Inequality

Figure 4 reports the conditional variance decomposition for the Gini coefficients of consumption and wealth as measures of inequality. Both decompositions indicate that inequality dynamics are shaped by a broad set of structural shocks rather than being dominated by a single source.

The decomposition of the wealth Gini shows that technology-related shocks account for the largest share of variation, explaining 31.1 percent of the total. Price and wage markup shocks follow, contributing 15.5 percent and 25.9 percent, respectively. The prominence of markup shocks is intuitive, as they affect households differently across

asset payoffs.

Figure 4 Conditional Variance Decomposition of Inequality Measures



Notes: Conditional variance decompositions of Consumption Gini and Wealth Gini at business cycle frequencies (6–32 quarter forecast horizon) based on the estimated model. The coloured areas indicate the share of the variance in the illustrated variable due to an individual shock.

the wealth distribution through changes in wages and profits. Monetary policy shocks are the next major contributor, accounting for 12.4 percent of the variation. Since monetary policy affects households directly through the Euler equation, it naturally generates heterogeneity in wealth outcomes by affecting asset holders and non-asset holders differently. Asset price shocks contribute more modestly, explaining 6.2 percent of the variation. This suggests that while asset price fluctuations influence short-run portfolio valuations, their aggregate contribution to long-run wealth inequality remains limited.

For the consumption Gini, technology shocks, investment-specific technology shocks, and price and wage markup shocks each explain roughly 20 percent of the total variance. The near-uniform contributions across these supply-side forces indicate that households are affected heterogeneously along the distribution. Monetary policy accounts for about 13 percent, consistent with heterogeneous exposure to interest-rate changes as in Auclert (2019). The asset price shock explains only 5.9 percent, which mirrors the wealth results. Although the shock affects equity holders differently than the average household, equity holders form a relatively small group, and their consumption responds with limited volatility.

Comparison to the literature Smets and Wouters (2007) showed that in representative-agent DSGE models, risk-premium and expenditure shocks account for the majority of short-run output fluctuations. In contrast, technology and markup shocks dominate at longer horizons. Justiniano, Primiceri and Tambalotti (2011) show that at business-cycle frequencies, 60 percent of output variation can be explained by shocks to the marginal efficiency of investment, and 25 percent by technology shocks. Consumption variation is

explained by intertemporal preference shocks and technology shocks that account for 55 percent and 31 percent of the variation, respectively. Our heterogeneous-agent results indicate that supply-side shocks, particularly investment-specific and neutral technology shocks, drive most consumption variation. This result is closer to those obtained by Auclert, Rognlie and Straub (2020) and Bayer, Born and Luetticke (2024), which place great importance on supply-side shocks for output and consumption.

Regarding inequality, volatility in the wealth Gini is mainly explained by supply-side shocks, whereas volatility in the consumption Gini is explained in equal parts by a variety of shocks. Monetary and asset price shocks have moderate effects, while technology and markup shocks matter more because they shift income and prices unevenly across households. Consistent with Auclert, Rognlie and Straub (2020) and Bayer, Born and Luetticke (2024), our results imply that supply-side disturbances are central to both aggregate and distributional dynamics. In contrast, valuation shocks only drive short-run fluctuations in asset markets.

6 Historical Analysis and the Impact of Monetary Policy

Since asset premia reflect households' exposure to aggregate risk, changes in the sources of aggregate risk over time imply corresponding variation in asset premia. This section examines the channels that drive this variation and isolates the role of monetary policy in shaping asset premia.

6.1 Historical analysis of asset premia

To begin, I investigate whether the model can account for historical variation in asset premia arising from shifts in the underlying sources of aggregate risk. Specifically, I re-estimate all model parameters for two distinct subperiods, 1979:Q3–1999:Q4 and 2000:Q1–2019:Q4. The first period corresponds to the Great Moderation following Volcker's appointment, while the second is characterized by greater international integration. The re-estimations use the same priors as in the main analysis. Appendix IV reports the Gelman and Rubin (1992) convergence statistics for both estimations, which indicate convergence to the posterior distribution.

Parameter estimates reported in Appendix VI show that the pre-2000 period is characterized by higher shock volatility and lower persistence than the model estimated on the full sample. An exception is the technology shock, which remains more persistent and continues to account for most of the business cycle variation in this period.

Table 6 Annualized Asset Premia in Excess of the 3-month Government Bond Return

	1979-Q3 to 1999-Q4			2000-Q1 to 2019-Q4	
Asset	**Data** (%)	**Model** (%)	**Alt. MP (%)**	**Data** (%)	**Model** (%)
Equity	8.21	5.87	6.02	3.27	4.56
Bond 6m	0.19	0.27	0.29	0.11	0.08
Bond 1y	0.36	0.57	0.60	0.21	0.19
Bond 2y	0.71	0.99	1.02	0.45	0.38
Bond 5y	1.29	1.40	1.43	1.11	0.63
Bond 10y	1.77	1.66	1.71	1.76	0.83
Bond 20y	2.18	2.14	2.20	2.31	1.14

Notes: Annualized premia for the estimated heterogeneous-agent model from re-estimated full models for the subperiods 1979-1999 and 2000-2019 compared to the data counterparts and with an alternative monetary policy rule (Alt. MP). Premia are computed following Auclert et al. (2024): $\frac{R_1 - R_0}{R} \approx -X\,\bar{\lambda}\,\sigma^2$, where X is the ex-post variation of an asset's excess return over the three-month bond return and $\bar{\lambda}$ is the aggregate pricing kernel. The equity premium is the sample mean of annualized stock excess returns over a long-term bond, proxied by the return on a ten-year zero-coupon bond. Term premia are the excess returns on zero-coupon bonds at constant maturities relative to the three-month zero-coupon bond. The equity return series matches those used in the estimation. Zero-coupon yields are from the Board of Governors of the Federal Reserve System.

The post-2000 period, in contrast, features lower shock volatility, more persistent but smaller shocks, a stronger and more stable monetary policy response to inflation, and reduced wage rigidities. In this later period, the government expenditure shock becomes highly persistent and accounts for most of the variation at business-cycle frequencies. Consistent with these estimates, Table 11 in Appendix VI shows that macroeconomic aggregates were more volatile in the first subperiod than in the second.

Table 6 compares the model-implied premia with their empirical counterparts after re-estimating the risk structure and policy parameters. Columns two and five report the empirical asset premia for the two subperiods, while columns three and six list the corresponding model-implied premia. For the pre-2000 period, the model explains much of the observed equity premium (5.87 percent versus 8.21 percent) and closely matches the term premium across maturities. For the post-2000 period, it produces an equity premium of 4.56 percent—slightly above the empirical value of 3.27 percent, and fits the short end of the term structure but not the steepening at longer maturities. Overall, the model does not match the exact levels but captures the cross-period ordering, replicates the yield-curve slope in the first subperiod, and remains close for shorter maturities in the second. Qualitatively, it reproduces how changes in underlying risk factors shape the evolution of equity premia across periods, and quantitatively, it tracks the behavior

of term premia. In line with the higher macroeconomic risk before 2000, the model generates larger asset premia in the first subperiod than in the second.

6.2 The Impact of Monetary Policy on Asset Premia

The historical analysis raises the question of whether the observed variation in asset premia is driven by changes in the nature of aggregate risk itself or by shifts in policy parameters and macroeconomic frictions. To address this, I next analyze how monetary policy shapes asset premia by altering the transmission of aggregate risk. Using the mean posterior estimates reported in Table 3 from the model estimated over the full sample, I vary the policy stance by changing the responses to inflation (ϕ_π) and output (ϕ_y). This approach isolates the effects of a more hawkish or dovish monetary policy while keeping the size of the underlying shocks constant.

Table 7 reports annualized asset premia and business-cycle volatilities of aggregate variables under alternative monetary policy stances. A stronger response to inflation ϕ_π raises asset premia across the board. In contrast, a stronger response to output ϕ_y lowers most premia. The intuition follows standard textbook logic. When business cycle risk is driven mainly by supply side shocks, a higher coefficient ϕ_π stabilizes inflation volatility at the cost of higher volatility in aggregate variables. Households that absorb the residual risk in asset markets then face more nondiversifiable risk and demand higher premia. On the contrary, raising the coefficient on output growth, ϕ_y, stabilizes output and reduces the risk borne in asset markets, thereby lowering premia. Consequently, asset premia move with monetary policy because it alters the residual aggregate risk households must bear.

I can use this insight to examine how changes in the monetary policy stance across the two subperiods affect asset premia. The increase in the inflation response coefficient ϕ_π from 2.156 to 2.314 and the decrease in the output response coefficient ϕ_Y from 1.69 to 0.114 should, in principle, raise asset premia in the post-2000 period relative to the pre-2000 period. Column three of Table 6 shows how the model implied premia change when I use the mean posterior estimates from the pre-2000 period for all parameters except the monetary policy coefficients ϕ_π and ϕ_Y, which are replaced by their post-2000 values. For all assets, the model implied premia increase, confirming that a stronger reaction to inflation and a weaker response to output growth raise asset premia in an economy where supply shocks are dominant. This exercise also suggests that the observed difference between the two subperiods cannot be explained solely by changes in monetary policy but is likely driven by shifts in the underlying aggregate risk structure.

Table 7 Annualized Asset Premia under varying Monetary Policy Stance

	Coefficient for Inflation (ϕ_π)			**Coefficient for Output** (ϕ_y)		
Premia	$\phi_\pi = 1.1$	$\phi_\pi = 1.69$	$\phi_\pi = 3.0$	$\phi_y = 0.0$	$\phi_y = 0.17$	$\phi_y = 0.5$
Equity	4.37	4.92	5.28	5.02	4.92	4.77
Bond 1y	0.17	0.24	0.34	0.27	0.24	0.21
Bond 10y	0.83	1.71	2.07	1.72	1.71	1.72
Std. Dev.	$\phi_\pi = 1.1$	$\phi_\pi = 1.69$	$\phi_\pi = 3.0$	$\phi_y = 0.0$	$\phi_y = 0.17$	$\phi_y = 0.5$
$100\sigma(c)$	0.53	0.55	0.61	0.56	0.55	0.53
$100\sigma(\pi)$	3.12	2.08	1.14	6.14	6.12	6.10
$100\sigma(r^{eq})$	6.10	6.12	6.20	2.16	2.08	1.94
$100\sigma(r^{10y})$	0.72	0.75	0.81	0.76	0.75	0.75

Notes: Annualized asset premia and standard deviations of selected variables over the business cycle frequency computed with the posterior mean parameters of the estimated heterogeneous agent model for the full sample period. The standard deviations σ are computed for variables c, π, r^{eq}, and r^{10y} referring to consumption growth, the price inflation rate, the equity return, and the 10-year bond return. The table varies the monetary policy responses to inflation, ϕ_π, and output, ϕ_y. Premia are computed following Auclert et al. (2024): $\frac{R_1 - R_0}{R} \approx -X\,\bar{\lambda}\,\sigma^2$, where X denotes the ex-post variation of an asset's excess return relative to the three month bond and $\bar{\lambda}$ denotes the aggregate pricing kernel. The variance over the business cycle frequency is computed based on Uhlig (2001).

This insight contrasts with the macro-finance literature based on representative agent models. While Kung (2015), Campbell, Pflueger and Viceira (2020), and Bianchi, Kung and Tirskikh (2023) highlight the role of monetary policy in shaping asset prices through the correlation of the stochastic discount factor with inflation, growth, and asset returns, the present heterogeneous-household model shifts the focus to the distribution of risk and to how policy shapes the residual aggregate risk households are exposed to. Finally, the insight also relates to Gornemann, Kuester and Nakajima (2016): asset premia increase with hawkish monetary policy, thereby increasing income for wealthy households while also exposing them to larger aggregate risk. Consequently, the welfare effects are unclear but could be an interesting future research avenue.

7 Conclusion

This paper develops and estimates a quantitative heterogeneous-agent New Keynesian model with endogenous portfolio choice and nonfundamental asset price shocks. By introducing noise traders in a segmented equity market, the model captures fluctuations in asset prices that are disconnected from economic fundamentals.

The model is able to explain the volatility of equity returns and replicate the empirical equity premium. Nonfundamental shocks are crucial for these results. They account for 79 percent of the variance in equity returns and explain 44 percent of the model-implied equity premium. This result arises because disproportionately wealthy equity holders face substantial consumption volatility due to large fluctuations in returns, even though they are otherwise well-insured. The model thus bridges a gap in the literature by showing that nonfundamental asset price risk can generate sizable premia in a setting with realistic heterogeneity and limited aggregate effects. These findings suggest that the pricing of risk in financial markets is determined not only by economic fundamentals but also by the interaction of nonfundamental shocks with portfolio heterogeneity and households' limited ability to share risk.

Besides matching the equity premium, the paper also explains the upward-sloping term premium. Returns on short-term bonds are mainly influenced by monetary policy, whereas returns on long-term bonds are primarily drive by persistent technology shocks. Low-wealth households that hold short-term bonds for consumption smoothing are only weakly affected by monetary policy shocks, which rationalizes the small term premia at short maturities. In contrast, holders of long-maturity bonds experience consumption volatility following persistent technology shocks, so they require larger compensation, leading to sizable term premia at longer maturities.

While these nonfundamental shocks are essential for explaining the equity premium and generating substantial volatility in equity prices, their aggregate macroeconomic effects are limited. This limited effect is due to the relatively small share of equity in total household wealth and equity holders' low marginal propensities to consume out of wealth. As a result, nonfundamental fluctuations account for little of the variation in aggregate consumption, investment, and inequality.

The paper also provides insights into how historical shifts in aggregate risk affect asset premia and how monetary policy shapes them. The re-estimated model shows that asset premia are higher in the post-Volcker, pre-2000 period, when overall macroeconomic volatility is elevated, and lower in the post-2000 period, when volatility is lower. Monetary policy affects asset premia by altering how aggregate shocks translate into volatility in macroeconomic variables. The model identifies supply-side shocks as the main drivers of this volatility. A more hawkish monetary policy ultimately raises asset premia by increasing macroeconomic fluctuations.

Future research could build on this framework to study how nonfundamental fluctuations in capital prices and quantitative easing affect the macroeconomy, the wealth and income distribution, and the formation of asset premia.

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Appendix

I Appendix: Derivations for Equity Price

This section illustrates the derivation of the equilibrium equity price in the main text, and illustrates an alternative derivation based on an incomplete information setting.

I.1 Derivation of Equilibrium Equity Price

For each equity j, market clearing requires that aggregate demand equals the (normalized) unit supply:

$$\int_0^1 \theta_{ljt}\, dl \;=\; 1. \tag{32}$$

From the fundamental trader problem, the optimal demand for equity j is

$$\theta^F_{ljt} \;=\; -\,q_{jt} \;+\; \mathbb{E}_t\left[\frac{d_{jt+1}+q_{jt+1}}{1+r_{t+1}}\right] \quad \text{for all } l \in [0,\nu], \tag{33}$$

while noise traders follow the rule

$$\theta^N_{ljt} \;=\; \tilde{\xi}_t \;+\; \epsilon^\theta_{ljt} \quad \text{for all } l \in (\nu,1], \tag{34}$$

where ϵ^θ_{ljt} is iid with zero mean across l (and j). Integrating (33) over the mass ν of fundamental traders and (34) over the mass $1-\nu$ of noise traders yields

$$\int_0^\nu \theta^F_{ljt}\, dl = \nu\left(-\,q_{jt} + \mathbb{E}_t\left[\frac{d_{jt+1}+q_{jt+1}}{1+r_{t+1}}\right]\right), \tag{35}$$

$$\int_\nu^1 \theta^N_{ljt}\, dl = (1-\nu)\tilde{\xi}_t \;+\; \underbrace{\int_\nu^1 \epsilon^\theta_{ljt}\, dl}_{=0}. \tag{36}$$

The trader-stock specific shock ϵ^θ_{ljt} washes out when averaged over traders due to its iid structure. Substituting (35) and (36) into (32) gives

$$\nu\left(-\,q_{jt} + \mathbb{E}_t\left[\frac{d_{jt+1}+q_{jt+1}}{1+r_{t+1}}\right]\right) \;+\; (1-\nu)\tilde{\xi}_t \;=\; 1. \tag{37}$$

Solving (37) for q_{jt} yields

$$q_{jt} \;=\; \mathbb{E}_t\left[\frac{d_{jt+1}+q_{jt+1}}{1+r_{t+1}}\right] \;+\; \frac{(1-\nu)\tilde{\xi}_t - 1}{\nu}. \tag{38}$$

Define the effective nonfundamental asset-price term as

$$\xi_t \equiv \frac{(1-\nu)\tilde{\xi}_t - 1}{\nu}, \tag{39}$$

then (38) becomes

$$q_{jt} = \mathbb{E}_t\left[\frac{d_{jt+1} + q_{jt+1}}{1 + r_{t+1}}\right] + \xi_t, \tag{40}$$

which matches equation (2) in the main text. By assumption, ξ_t follows the AR(1) process $\xi_t = \rho_q \xi_{t-1} + \epsilon_t^q$ with $\epsilon_t^q \sim \mathcal{N}(0, \sigma_q^2)$. In a symmetric equilibrium with identical firms, $q_{jt} = q_t$ and $d_{jt} = d_t$ for all j. Aggregating (40) across j yields the index-fund pricing equation

$$q_t = \mathbb{E}_t\left[\frac{d_{t+1} + q_{t+1}}{1 + r_{t+1}}\right] + \xi_t, \tag{41}$$

which coincides with equation (3).

I.2 Alternative Microfoundation of Asset Price Shock

This subsection provides an alternative microfoundation of asset price shocks based on incomplete information as in Futia (1981), Singleton (1986), Bacchetta and Wincoop (2006), Angeletos and Lian (2016), and Rondina and Walker (2021). Each trader $m \in [0,1]$ observes a noisy signal about the future payoff of each equity $j \in [0,1]$, given by:

$$x_{mjt} = d_{jt+1} + u_{mjt}, \quad \text{where } u_{mjt} \sim \mathcal{N}(\tilde{\xi}_t, \sigma_u^2).$$

The noise term u_{mjt} contains a cross-sectionally common distortion $\tilde{\xi}_t$, which biases the beliefs of all traders in the same direction.

Traders with Imperfect Information. Each trader lives for two periods,[22] is risk-neutral, discounts the future at the risk-free rate $1 + r_{t+1}$, and incurs quadratic disutility from monitoring firm-specific signals. Each trader chooses a portfolio allocation $\{\theta_{mjt}\}_{j\in[0,1]}$ to maximize:

$$U_{mt} = \max_{\{\theta_{mjt}\}} \int_0^1 \left[-q_{jt}\theta_{mjt} + \mathbb{E}_{mt}\left(\frac{d_{jt+1} + q_{jt+1}}{1 + r_{t+1}}\right)\theta_{mjt} - \frac{1}{2}\theta_{mjt}^2\right] dj,$$

[22] By assuming that traders only live for two periods, higher-order believes beliefs of traders about next periods price become irrelevant. This assumption makes the solution more tractable, but as Bacchetta and Wincoop (2006) show in their paper, does not change the implications.

where $\mathbb{E}_{mt}[\cdot]$ denotes trader m's subjective expectation, based on the signal x_{mjt}. The optimal portfolio demand satisfies:

$$\theta_{mjt} = \mathbb{E}_{mt}\left[\frac{d_{jt+1} + q_{jt+1}}{1 + r_{t+1}}\right] - q_{jt}.$$

Equilibrium Asset Prices. Market clearing requires that the average demand equals the unit supply of each equity, that is:

$$\int_0^1 \theta_{mjt} dm = 1.$$

Substituting the demand expression yields the asset pricing equation:

$$q_{jt} = \bar{\mathbb{E}}_t\left[\frac{d_{jt+1} + q_{jt+1}}{1 + r_{t+1}}\right] - 1,$$

where $\bar{\mathbb{E}}_t[\cdot]$ denotes the cross-sectional average of individual expectations.

Belief Distortions and Nonfundamental Prices. Bayesian updating under normally distributed noise implies that all traders share a distorted belief about the average payoff:

$$\bar{\mathbb{E}}_t\left[\frac{d_{jt+1} + q_{jt+1}}{1 + r_{t+1}}\right] = \mathbb{E}_t^{\text{true}}\left[\frac{d_{jt+1} + q_{jt+1}}{1 + r_{t+1}}\right] + \frac{\tilde{\xi}_t}{1 + r_{t+1}}.$$

Substituting this into the pricing equation yields:

$$q_{jt} = \mathbb{E}_t^{\text{true}}\left[\frac{d_{jt+1} + q_{jt+1}}{1 + r_{t+1}}\right] + \xi_t,$$

where the effective asset price shock is defined as:

$$\xi_t \equiv \frac{\tilde{\xi}_t}{1 + r_{t+1}} - 1.$$

As in the main text, we assume ξ_t follows a stationary AR(1) process:

$$\xi_t = \rho_q \xi_{t-1} + \epsilon_t^q, \quad \epsilon_t^q \sim \mathcal{N}(0, \sigma_q^2).$$

Symmetric Equilibrium and Index Fund Pricing. Assuming that all equities are symmetric and deliver identical payoffs, the price of the equity index fund satisfies:

$$q_t = \mathbb{E}_t^{\text{true}} \left[\frac{d_{t+1} + q_{t+1}}{1 + r_{t+1}} \right] + \xi_t,$$

which corresponds exactly to equation (3) in the main text. Hence, distorted beliefs due to incomplete information can rationalize the same reduced-form expression for nonfundamental price movements as in the model with noise traders.

Implications for Returns. As before, asset price fluctuations translate into excess returns through:

$$r_t^e = \frac{q_t - q_{t-1} + d_t}{q_{t-1}},$$

such that nonfundamental shocks affect both prices and returns, even in the absence of changes to dividends or discount factors.

II Appendix: Derivations of the endogenous portfolios

This section derives the results of Auclert et al. (2024) in a unified manner.

Setting and perturbation

There exists a continuum of heterogeneous agents with index i who can allocate their wealth a_i to up to $K+1$ assets. An asset k has supply A^k and stochastic payoff $x^k(\epsilon)$, where $\epsilon \equiv (\epsilon_1, ..., \epsilon_Z)$ denotes the vector of Z exogenous shocks. We suppose that $\epsilon_Z = \sigma \bar{\epsilon}_Z$, with $\bar{\epsilon}_Z \sim N(0, \overline{\sigma}_Z^2)$, such that σ is the common volatility that exists in the economy. Denoting the value function of household i by W_i and given the price of asset k as p^k, the problem of household i is

$$\max_{a_i^k} \mathbb{E}_\epsilon \left[W_i \left(\sum_{k=0}^{K} x^k(\epsilon) a_i^k, \epsilon \right) \right] \tag{42}$$

$$\text{s.t.} \quad \sum_{k=0}^{K} p^k a_i^k = a_i \tag{43}$$

with $W_i(a', \epsilon) = \mathbb{E}_{s',s} \left[V(a', s', \epsilon)^{1-\gamma} \right]^{\frac{1}{1-\gamma}}$ denoting the weighted certainty equivalence operator, where s' denotes the idiosyncratic risk. Denoting the Lagrange multiplier on i's

budget constraint by γ_i, the problem has the first-order conditions

$$\mathbb{E}_\epsilon \left[\frac{x^k(\epsilon)}{p^k} \frac{W_i'(\epsilon)}{\gamma_i} \right] = 1 \tag{44}$$

which must hold for every i and for every k. Writing di for distribution of agents i, market clearing in all asset markets imposes:

$$\int a_i^k di = A^k \quad \forall k. \tag{45}$$

Given primitives a_i and W_i, as well as the parameter σ, an equilibrium is a set of prices for each asset p^k and Lagrange multiplier for each agent γ_i, such that the optimality conditions (44) are satisfied for each (i,k) pair, and all asset markets clear, i.e. (45) holds for all k.

We now work out the implications of these equations for a perturbation in σ up to the second order. We write $p^k(\sigma)$ and $\gamma_i(\sigma)$ for the solution at a given σ and study their second-order Taylor expansion around $\sigma = 0$. We note that, given that the distribution of ϵ is symmetric, these must be even functions of σ: $p^k(-\sigma) = p^k(\sigma)$ and $\gamma_i(-\sigma) = \gamma_i(\sigma)$. This implies, in particular, that $\frac{d\gamma_i}{d\sigma} = \frac{dp^k}{d\sigma} = 0$[23], a result that we will use several times below.

Zero-th and first-order perturbation: Applying (44) at $\sigma = 0$, we find $\gamma_i / W_i' = x^k / p^k$ for all i and k, where p^k is short-hand for $p^k(0)$, γ_i for $\gamma_i(0)$, x^k for $x^k(0)$, and W_i' for $W_i'(\sum_{k=0}^K x^k a_i^k, 0)$. Hence, the returns on all assets must equal a common constant R, and this is also the rate entering the Euler equation of all agents:

$$\gamma_i / W_i' = x^k / p^k = R \tag{46}$$

In particular, $\sum_{k=0}^K x^k a_i^k$ is also just $R \sum_{k=0}^K p^k a_i^k = R a_i$. Equation (46) gives the usual result that, with no aggregate uncertainty, all assets must have equal returns.

Next, differentiating (44) with respect to σ (and around $\sigma = 0$) gives us

$$\mathbb{E}\left[\frac{dx^k}{d\sigma} W_i' + x^k \frac{dW_i'}{d\sigma} \right] = \frac{d\gamma_i}{d\sigma} p^k + \gamma_i \frac{dp^k}{d\sigma} \tag{47}$$

[23] Up to first order, the portfolios are not determined such that the portfolio constraints do not bind. The only constraint that might bind is the constraint on total wealth.

Given the definition $x^k(\epsilon) = x^k(\sigma\overline{\epsilon}_1, ..., \sigma\overline{\epsilon}_Z)$, and $W_i(\sum_{k=0}^K x^k(\sigma\overline{\epsilon})a_i^k, \sigma\overline{\epsilon})$, we have that

$$\frac{dx^k}{d\sigma} = \sum_{z=1}^{Z} \frac{\partial x^k}{\partial \epsilon_z}\overline{\epsilon}_Z \quad \text{and} \quad \frac{dW_i'}{d\sigma} = \sum_{z=1}^{Z} \frac{dW_i'}{d\epsilon_z}\overline{\epsilon}_z \tag{48}$$

where we have defined the total deriviate of W_i' with respect to ϵ_z as

$$\frac{dW_i'}{d\epsilon_z} \equiv W_i'' \sum_{k=0}^{K} \frac{\partial x^k}{\partial \epsilon_z} a_i^k + \frac{\partial W_i'}{\partial \epsilon_z}$$

Since $\mathbb{E}[\overline{\epsilon}_z] = 0$, using equation (48) to substitute into (47), we see that the left-hand side is zero. The right-hand side of (47) is also zero, given our symmetry result above, so equation (47) holds regardless of portfolios.

Second-order perturbation: Now, differentiating (47) with respect to σ gives us:

$$\mathbb{E}\left[\frac{d^2x^k}{d\sigma^2}\right] W_i' + 2\mathbb{E}\left[\frac{dx^k}{d\sigma}\frac{dW_i'}{d\sigma}\right] + x^k\mathbb{E}\left[\frac{d^2W_i'}{d\sigma^2}\right] = \frac{d^2\gamma_i}{d\sigma^2}p^k + 2\frac{d\gamma_i}{d\sigma}\frac{dp^k}{d\sigma} + \gamma_i\frac{d^2p^k}{d\sigma^2} \tag{49}$$

Using our symmetry results from above, and dividing all entries by $x^kW_i' = \gamma_i p^k$ from (46), we can write this simply as:

$$\mathbb{E}\left[\frac{dx^k/x^k}{d\sigma}\frac{dW_i'/W_i'}{d\sigma}\right] = \alpha_i + \beta^k, \tag{50}$$

where α_i, which only depends on household i, β^k, which only depends on asset k, and δ_i^k, which depends on both are defined as

$$\alpha_i \equiv \frac{1}{2}\left(\frac{d^2\gamma_i/\gamma_i}{d\sigma^2} - \mathbb{E}\left[\frac{d^2W_i'/W_i'}{d\sigma^2}\right]\right)$$
$$\beta^k \equiv \frac{1}{2}\left(\frac{d^2p^k/p^k}{d\sigma^2} - \mathbb{E}\left[\frac{d^2x^k/x^k}{d\sigma^2}\right]\right)$$

Using (48), and the fact that $\mathbb{E}[\overline{\epsilon}\overline{\epsilon}'] = \Sigma$, we can rewrite (50) as

$$\sum_{z=1}^{Z} \frac{\partial x^k/x^k}{\partial \epsilon_z}\frac{dW_i'/W_i'}{d\epsilon_z}\overline{\sigma}_z^2 = \alpha_i + \beta^k \quad \forall\, i,k \tag{51}$$

We note that this applies to the product of two first derivatives, and therefore, intuitively, places restrictions on the relationship between the impulse response of returns and marginal utilities. Finally, using (51) for asset k relative to asset 0 (where we note that 0 could correspond to any reference asset in the economy), we obtain:

$$\sum_{z=1}^{Z}\left(\frac{\partial x^k/x^k}{\partial \epsilon_z}-\frac{\partial x^0/x^0}{\partial \epsilon_z}\right)\frac{dW_i'/W_i'}{d\epsilon_z}\overline{\sigma}_z^2=\underbrace{\beta^k-\beta^0}_{b^k}\quad\forall\, i,k \tag{52}$$

Equation (52) says that all households equalize their average sensitivity to shocks z, interacted with the relative returns on asset k, to a k-specific term b^k. We will soon see that this term has the interpretation of a relative risk premium on asset k. Stacking $\mathbf{b}\equiv(b^1,...,b^K)'$ as a $K\times 1$ vector of relative risk premia, $\boldsymbol{\lambda}_i\equiv(\frac{dW_i'/W_i'}{d\epsilon_1},...,\frac{dW_i'/W_i'}{d\epsilon_Z})'$ as a $Z\times 1$ vector of sensitivities of marginal utility to each shock, defining the $Z\times K$ matrix $\mathbf{X}$ with elements equal to the relative returns of each asset to each shock $X_{zk}\equiv\frac{\partial x_k/x_k}{\partial\epsilon_Z}-\frac{\partial x_0/x_0}{\partial\epsilon_Z}$, and letting $\boldsymbol{\Sigma}$ denote the $Z\times Z$ matrix with $\overline{\sigma}_z^2$ on its diagonal, equation (52) becomes:

$$\mathbf{X}'\boldsymbol{\Sigma}\boldsymbol{\lambda}_i=\boldsymbol{b}\quad\forall\, i \tag{53}$$

Equation (53) is core for the portfolio choice, which I illustrate next.

Complete markets

Suppose that $K=Z$, such that the number of assets equals the number of shocks plus one. This effectively allows households to insure against all aggregate shocks by taking respective portfolio positions. We say that this corresponds to complete markets with respect to aggregate risk. Then $\mathbf{X}$ is a square matrix. Additionally, suppose the following assumptions are fulfilled:

Assumption 1 (Spanning)**.** *The rows of* $\mathbf{X}$ *are linearly independent.*

and

Assumption 2 (Constraints)**.** *There are no portfolio constraints, such that* $\eta_{it}=\delta_i^k=0$ *and* $\boldsymbol{\Theta}'\boldsymbol{\eta}_i=\mathbf{0}_K$.

Assumption 1 says that the relative returns across assets vary sufficiently across shocks, while assumption 2 abstracts from portfolio constraints. Under the first assumption, the $Z\times Z$ matrix $\mathbf{X}'\boldsymbol{\Sigma}$ is invertible, while the second assumption abstracts from idiosyncratic

binding constraints. Condition (53) can therefore be rewritten:

$$\boldsymbol{\lambda}_i = (\mathbf{X}')^{-1}\boldsymbol{\Sigma}^{-1}\mathbf{b} \equiv \boldsymbol{\lambda}, \tag{54}$$

which yields the first main result.

Proposition 1. *Suppose that $K = Z$ and assumptions 1 and 2 hold. Then for each shock z, there exists a λ_z such that*

$$\frac{dW_i'/W_i'}{d\epsilon_z} = \lambda_z \quad \forall\, i. \tag{55}$$

Proposition 1 provides us with a simple test of portfolio optimality in a setting where $K = Z$. To understand the test, note that standard first-order methods allow us relatively easily to solve for steady-state x^k, W_i, as well as $\frac{x^k}{\partial \epsilon_z}$ and $\frac{dW_i'}{d\epsilon_z}$ for given shocks z, conditional on given incoming portfolios $\{a_i^k\}$ for all agents. With these objects, one can form the matrix of relative returns $\mathbf{X}$ to test if the spanning assumption 1 is satisfied, and then test whether $\frac{dW_i'/W_i'}{d\epsilon_z}$ are equalized across agents i for all shocks z. If so, proposition 1 tells us that the portfolios are optimal.

Proposition 1 also implies a method for solving for optimal portfolios directly. Suppose that $\overline{a}_i^k$ is an exogenous portfolio and let t_i be the excess payoff from another portfolio a_i^k such that

$$t_i \equiv \sum_{k=0}^{K} x^k(\epsilon)(a_i^k - \overline{a}_i^k). \tag{56}$$

Moreover, let $\overline{W}_i\left(\sum_{k=0}^{K} x^k(\epsilon)\overline{a}_i^k, \boldsymbol{\epsilon}\right)$ denote the value function under the exogenous portfolio, whereas $W_i(t_i, \boldsymbol{\epsilon}) \equiv \overline{W}_i\left(\sum_{k=0}^{K} x^k(\epsilon)\overline{a}_i^k + t_i, \epsilon\right)$ denotes the value function under the portfolio a_i^k. With complete markets and assumptions 1 and 2 in place, households portfolios should satisfy the risk-sharing condition (55). We can find the corresponding excess payoff t_i, by imposing that it satisfies the risk-sharing condition. Given the exogenous portfolio $\overline{a}_i^k$, we can approximate the risk-sharing condition at the optimal portfolio around the utility change in the exogenous portfolio case as

$$\frac{d\overline{W}_i'/\overline{W}_i'}{d\epsilon_z} + \frac{\overline{W}_i''}{\overline{W}_i'}\frac{dt_i}{d\epsilon_z} = \lambda_z. \tag{57}$$

The first term on the right-hand side of (57) refers to the direct exposure to shocks under exogenous portfolios, whereas the second term denotes the "transfer" exposure to shocks under a portfolio that achieves optimal aggregate risk-sharing. Intuitively,

equation (57) provides a condition to solve for transfers contingent on shocks $dt_i/d\epsilon_z$:

$$\frac{dt_i}{d\epsilon_z} = \frac{\overline{W}_i'}{\overline{W}_i''}\left(\lambda_z - \frac{d\overline{W}_i'/\overline{W}_i'}{d\epsilon_z}\right) \tag{58}$$

and since transfers have to sum to zero, $\int \frac{dt_i}{d\epsilon_z} di = 0$, we obtain:

$$\lambda_z = \left(\int \frac{\overline{W}_i'}{\overline{W}_i''} di\right)^{-1} \int \frac{\overline{W}_i'}{\overline{W}_i''} \frac{d\overline{W}_i'/\overline{W}_i'}{d\epsilon_z} di. \tag{59}$$

We can use these two equations to derive λ_z via equation (59) and then obtain excess returns via equation (58). From the definition of the excess returns (56), we then obtain the relation between transfers and the endogenous portfolios that ensures optimal insurance against aggregate risk:

$$\frac{dt_i}{d\epsilon_z} = \sum_{k=0}^{K} \frac{dx^k}{d\epsilon_z}(\epsilon)(a_i^k - \overline{a}_i^k) \tag{60}$$

Using the definition of portfolio shares $\omega_i^k = \frac{a_i^k}{a_i}$ and $\overline{\omega}_i^k = \frac{\overline{a}_i^k}{a_i}$ we can rewrite equation (60) to

$$\begin{aligned}
\frac{\partial t_i}{\partial \epsilon_z} &= \sum_{k=0}^{K} \frac{\partial x^k}{\partial \epsilon_z}(\epsilon)(a_i^k - \overline{a}_i^k) \\
&= a_i \sum_{k=0}^{K} \frac{\partial x^k}{\partial \epsilon_z}(\epsilon)(\omega_i^k - \overline{\omega}_i^k) \\
&= a_i \sum_{k=1}^{K} \left(\frac{\partial x^k}{\partial \epsilon_z}(\epsilon) - \frac{\partial x^0}{\partial \epsilon_z}(\epsilon)\right)(\omega_i^k - \overline{\omega}_i^k).
\end{aligned}$$

Using the definition of $\mathbf{X}$ from above, and defining vectors $\boldsymbol{\omega}_i = (\omega_i^1, ..., \omega_i^K)'$, $\overline{\boldsymbol{\omega}}_i = (\overline{\omega}_i^1, ..., \overline{\omega}_i^K)'$, and $\mathbf{t}_i = (\frac{\partial t_i}{\partial \epsilon_1}, ..., \frac{\partial t_i}{\partial \epsilon_Z})'$, we can write the optimal portfolio weights as

$$\mathbf{t}_i = \mathbf{X}(\boldsymbol{\omega}_i - \overline{\boldsymbol{\omega}}_i)a_i \quad \Leftrightarrow \quad \boldsymbol{\omega}_i = \overline{\boldsymbol{\omega}}_i + \mathbf{X}^{-1}\frac{\mathbf{t}_i}{a_i} \tag{61}$$

For $K = 1$ (two assets) the relation becomes

$$\omega_i^1 = \overline{\omega}_i^1 + \frac{1}{a_i}\left(\frac{\partial x^1}{\partial \epsilon_z}(\epsilon) - \frac{\partial x^0}{\partial \epsilon_z}(\epsilon)\right)^{-1} \frac{dt_i}{d\epsilon_z}.$$

Finally, we can calculate the risk premia associated with the individual assets. We want to approximate risk-premia up to second order around $\sigma = 0$. First, let $R^k(\sigma) = \mathbb{E}\left[x^k(\sigma)\right]/p^k(\sigma)$ define the expected return on asset k. From equation (46), we have $R^k(0) = R$. The derivative of the expected return with respect to σ is

$$\frac{dR^k(\sigma)}{d\sigma} = \mathbb{E}\left[\frac{dx^k(\sigma)}{d\sigma}\right]\frac{1}{p^k(\sigma)} - \mathbb{E}\left[\frac{x^k(\sigma)}{p^k(\sigma)}\right]\frac{dp^k(\sigma)/p^k(\sigma)}{d\sigma} = 0, \tag{62}$$

which uses equation (48), $\mathbb{E}\left[\frac{dx^k}{d\sigma}\right] = 0$ and $\frac{dp^k}{d\sigma} = 0$ from our symmetry result. Finally, the second-order derivative of the expected return of asset k with respect to σ is

$$\begin{aligned}\frac{d^2R^k(\sigma)}{d\sigma^2} =& \mathbb{E}\left[\frac{d^2x^k(\sigma)}{d\sigma^2}\right]\frac{1}{p^k(\sigma)} - 2\mathbb{E}\left[\frac{dx^k(\sigma)}{d\sigma}\right]\frac{dp^k(\sigma)/p^k(\sigma)}{d\sigma}\frac{1}{p^k(\sigma)} \\ &- \mathbb{E}\left[x^k(\sigma)\right]\left[\frac{\frac{d^2p^k(\sigma)}{d\sigma^2}p^k(\sigma)^2 - 2\frac{dp^k(\sigma)}{d\sigma}p^k(\sigma)}{\left(p^k(\sigma)\right)^4}\right] \\ =& \mathbb{E}\left[\frac{d^2x^k(\sigma)}{d\sigma^2}\right]\frac{1}{p^k(\sigma)} - \mathbb{E}\left[\frac{x^k(\sigma)}{p^k(\sigma)}\right]\left[\frac{d^2p^k(\sigma)/p^k(\sigma)}{d\sigma^2}\right],\end{aligned} \tag{63}$$

where we have used again that the derivatives of the first order of payoffs $x^k(\sigma)$ and prices $p^k(\sigma)$ are zero. Note that $\frac{d^2R^k(\sigma)}{d\sigma^2} = -2R^k(\sigma)\beta^k$. A second-order Taylor expansion of the expected return $R^k(\sigma)$ around $\sigma = 0$ yields

$$R^k(\sigma) \approx R^k(0) + \frac{dR^k(0)}{d\sigma}\sigma + \frac{1}{2}\frac{d^2R^k(0)}{d\sigma^2}\sigma^2 = R - R\beta^k\sigma^2,$$

such that the relative risk premium of asset k against asset 0 has the second order expansion

$$\frac{R^k(\sigma) - R^0(\sigma)}{R} \approx -(\beta^k - \beta^0)\sigma^2 = -b^k\sigma^2. \tag{64}$$

We can use equation (52) and from proposition 1 equation (55) to obtain:

$$b^k = \sum_{z=1}^{Z} \underbrace{\left(\frac{\partial x^k/x^k}{\partial \epsilon_z} - \frac{\partial x^0/x^k}{\partial \epsilon_z}\right)}_{X_{zk}} \underbrace{\frac{dW_i'/W_i'}{d\epsilon_z}}_{\lambda_z} \overline{\sigma}_z^2 = \sum_{z=1}^{Z} X_{zk}\lambda_z\overline{\sigma}_z^2 \tag{65}$$

such that

Proposition 2. *Suppose markets are complete and assumptions (1) and (2) hold. Then, the risk premia of asset k relative to asset 0 satisfies, to second order*

$$\frac{R^k(\sigma) - R^0(\sigma)}{R} \approx -\sum_{z=1}^{Z} X_{zk}\lambda_z \overline{\sigma}_z^2 \sigma^2. \tag{66}$$

Proposition 2 allows us to approximate the risk premia on an assets k using only the information from a first-order perturbation.

III Appendix: Data sources and transformations

This section describes the data used for the calibration and in the Bayesian estimation of the model in the main text.

III.1 Calculation of Time-Series Averages for Calibration

To pin down steady-state targets, I compute time series for four aggregate ratios and for the depreciation rate using U.S. national accounts and market data, then take sample averages over 1954:Q1 to 2020:Q1. The data are obtained from FRED unless noted otherwise.

Capital-to-Output Ratio K_t/Y_t: Fixed assets (K1TTOTL1ES000) divided by GDP (FYGDP). Since capital is reported at an annual frequency, the series is multiplied by four to obtain a quarterly equivalent, computed as Capital-to-GDP $=$ Capital $\times\, 4/$GDP.

Debt-to-Output Ratio B_t/Y_t: Federal debt held by the public as percent of Gross Domestic Product (FYPUGDA188S). The series is multiplied by four to ensure consistency with the quarterly GDP concept.

Government Expenditure-to-Output Ratio G_t/Y_t: Government consumption and investment expenditures (GCEA) divided by GDP (FYGDP), both expressed in billions of dollars. The ratio is scaled to percentages as Expenditure-to-GDP $=$ GCEA/GDP $\times\, 100$.

Stock Market Value-to-Output Ratio $Q_t^{\mathbf{eq}}/Y_t$: Market value of listed domestic companies relative to GDP (DDDM01USA156NWDB). The series, is converted from a percent of GDP to a quarterly ratio using Stock-Market-to-GDP $=$ DDDM01USA156NWDB$/100 \times 4$.

Depreciation Rate δ_t: Computed from the ratio of total current-cost depreciation of fixed assets (M1TTOTL1ES000) to the corresponding capital stocks (K1TTOTL1ES000). The annual depreciation rate is defined as $\delta_{\text{annual}} = \text{Depreciation}/\text{Capital} \times 100$, and the quarterly depreciation rate used in the model equals $\delta = \delta_{\text{annual}}/4$.

The sample means of these variables serve as calibration targets for the steady state.

III.2 Calculation of Time-Series Averages for Government Debt

Maturity Structure of Government Debt $\omega^{(n)}, 1/\delta^{(n)}$: The calibration of the public debt structure is based on the historical database of De Graeve and Mazzolini (2023). I importing the quarterly, nominal market value of US government debt, which is broken down into 19 distinct maturity buckets ranging from 3 months to over 30 years. To convert these nominal values into real terms, each series is deflated using the GDP deflator (GDPDEF), which is sourced from the FRED database. Subsequently, for each quarter in the sample, the real value in each maturity bucket is divided by the total real value of all outstanding debt. This step normalizes the data, transforming the absolute monetary values into a time series of portfolio shares for each maturity, which sum to 100% in each period. The time-series average of these shares is then computed for each of the 19 maturities to establish a single, representative weight for the entire historical period. To create a more tractable structure for the model, these 19 buckets are then aggregated into seven broader tranches. For each of these seven final groups, the total share ($\omega^{(n)}$) is calculated by summing the average weights of the constituent maturities. The average duration ($1/\delta^{(n)}$) for each tranche is then determined by calculating the weighted average of the numerical maturities (e.g., "6M" is converted to 0.5 years) within that group, using their historical average shares as the weights. This procedure yields the final calibration parameters presented in Table 2.

III.3 Estimation on Time-Series Data

The observables used for the estimation can be summarized as

$$obs_t = \begin{bmatrix} \Delta \log(Y_t) \\ \Delta \log(C_t) \\ \Delta \log(I_t) \\ \Delta \log(w_t) \\ \Delta \log(q_t) \\ \Delta \log(d_t) \\ \log(N_t) \\ \log(1 + r_t^{eq}) \\ \log(\frac{1}{q_t^{3m}}) \\ \log(1 + \pi_t^p) \end{bmatrix} - \begin{bmatrix} \overline{\Delta \log(Y_t)} \\ \overline{\Delta \log(C_t)} \\ \overline{\Delta \log(I_t)} \\ \overline{\Delta \log(w_t)} \\ \overline{\Delta \log(q_t)} \\ \overline{\Delta \log(d_t)} \\ \overline{\log(N_t)} \\ \overline{\log(1 + r_t^{eq})} \\ \overline{\log(\frac{1}{q_t^{3m}})} \\ \overline{\log(1 + \pi_t^p)} \end{bmatrix}. \tag{67}$$

The Δ denotes the first difference between variables, and bars over variables denote the time-series averages. Except for the stock price and dividend series, all series are obtained from the St. Louise FED - FRED database. All data series from FRED are available at a quarterly frequency. The time series of stock prices, and dividends are obtained from the online database of Robert Shiller. The data was first generated for Shiller (1989), but was updated until today. The up-to-date time series can be accessed here. I extract monthly data on nominal stock prices Q_t^{eq} and dividends D_t from the online dataset and convert them to real series. I illustrate the transformation from monthly to quarterly frequency below and from nominal to real below.

Output Y_t: Sum of gross private domestic investment (GPDI), personal consumption expenditures for nondurable goods (PCND), durable goods (PCDG), and services (PCESV), and government consumption expenditures and gross investment (GCE) divided by the GDP deflator (GDPDEF) and the civilian noninstitutional population (CNP16OV).

Consumption C_t: Sum of personal consumption expenditures for nondurable goods (PCND), durable goods (PCDG), and services (PCESV) divided by the GDP deflator (GDPDEF) and the civilian noninstitutional population (CNP16OV).

Investment I_t: Gross private domestic investment (GPDI) divided by the GDP deflator (GDPDEF) and the civilian noninstitutional population (CNP16OV).

Real wage w_t: Hourly compensation in the nonfarm business sector (COMPNFB) divided by the GDP deflator (GDPDEF).

Hours worked N_t: Nonfarm business hours worked (HOANBS) divided by the civilian noninstitutional population (CNP16OV).

Inflation π_t: Computed as the log-difference of the GDP deflator (GDPDEF).

Nominal interest rate $\frac{1}{q_t^{3m}}$: Quarterly average of the effective federal funds rate (FEDFUNDS). From 2009-Q1 to 2015-Q4, I use the shadow federal funds rate of Wu and Xia (2016) instead of the federal funds rate, which was at the zero-lower bound.

Real stock prices q_t: The nominal stock price Q_t^{eq} (S&P Comp. P) is available at a monthly frequency in Robert Shiller's database. I convert the series to a quarterly frequency by taking the average over the realizations of the monthly stock price. Thereafter, the quarterly series is divided by the GDP deflator (GDPDEF) to obtain real stock prices.

Real dividends d_t: The nominal dividend D_t (Dividend) is available at a monthly frequency in Robert Shiller's database. I convert the series to a quarterly frequency by taking the average over the realizations of the monthly stock price. Thereafter, the quarterly series is divided by the GDP deflator (GDPDEF) to obtain the real dividend.

Real dividends d_t: The nominal dividend (Dividend) is available at a monthly frequency in Robert Shiller's database. I convert the series to a quarterly frequency by taking the average over the realizations of the monthly dividend. Thereafter, the quarterly series is divided by the GDP deflator (GDPDEF) to obtain the real dividend.

Real return r_t^{eq}: I use the quarterly nominal equity price Q_t^{eq} and the quarterly nominal dividend D_t to calculate the nominal equity return as $r_t^{eq,nom} = (Q_t^{eq} - Q_{t-1}^{eq})/Q_{t-1}^{eq} + D_t/D_{t-1}^{eq}$ based on the calculation of Jordà et al. (2019). I then convert the return from nominal to real by dividing it by the inflation rate obtained above: $1 + r_t^{eq} \equiv \frac{q_t + d_t}{q_{t-1}} = \frac{1+r_t^{eq,nom}}{1+\pi_t^p}$.

III.4 Calculation of Average Asset Premia

This subsection describes how I construct the data averages reported in Table 4. The calculation of the equity premium uses the monthly version of the real equity return

r_t^{eq} defined above. Term premia are based on Treasury yields at different maturities, described next.

Treasury yields $y_t^{(n)}$: I use monthly Treasury Constant Maturity rates from FRED for maturities 3M, 6M, 1Y, 2Y, 5Y, 10Y, and 20Y (series GS3M, GS6M, GS1, GS2, GS5, GS10, GS20).

Equity premium: Using the monthly real equity return r_t^{eq} based on Shiller (1989), I compute the monthly equity excess return as the difference between r_t^{eq} and the 10Y Treasury Constant Maturity yield. The equity premium is the sample average of this monthly excess return over the estimation window. I obtain an equity premium of 5.01 percentage points, which is in line with the averages reported by Jordà et al. (2019), among others.

Term premia: For each maturity $n \neq 3\text{M}$, the term premium is calculated as the average yield difference $tp_t^{(n)} = y_t^{(n)} - y_t^{(3\text{M})}$. All statistics are in annualized percentage points. The slope of the yield curve is strongly dependent on the country studied, as well as the period considered.[24] The estimates I obtain for the post-war U.S. term-premia are in line with the estimates used by other authors, see Campbell, Pflueger and Viceira (2020) for example.

IV Appendix: Estimation Diagnostics

To check convergence of the estimation, we use the Gelman and Rubin (1992) statistic and inspect the trace plots of the individual chains.

Table 8 reports the Gelman–Rubin potential scale reduction factor (Gelman and Rubin, 1992) for the estimation over the entire sample period, as well as for the subperiod from 1979 to 1999 and from 2000 to 2019. The statistic compares dispersion within each Markov chain to dispersion across chain means. When chains started from deliberately dispersed initial values have reached the common stationary distribution, these two sources of variation align and the statistic approaches one. Values meaningfully above one indicate that between chain dispersion remains elevated, which signals incomplete mixing. Following Vats and Knudson (2021), I use the conservative threshold of 1.01 to determine convergence. All parameters for all estimations fall well below

[24] See Kung (2015) for a discussion.

this threshold, supporting the conclusion that in all estimation exercises the chains have converged to the stationary posterior distribution.

Table 8 Gelman Rubin $\hat{R}$ statistics

Parameter	Full Sample	1979 to 1999	2000 to 2019
Structural Shocks			
σ_q	1.00119	1.0025	1.0021
ρ_q	1.00107	1.0035	1.0026
σ_ζ	1.00061	1.0020	1.0010
ρ_ζ	1.00063	1.0034	1.0029
σ_z	1.00071	1.0013	1.0016
ρ_z	1.00145	1.0022	1.0033
σ_r	1.00160	1.0018	1.0017
σ_I	1.00130	1.0021	1.0031
ρ_I	1.00270	1.0050	1.0052
σ_p	1.00075	1.0011	1.0017
ρ_p	1.00160	1.0087	1.0047
σ_w	1.00178	1.0032	1.0045
ρ_w	1.00125	1.0021	1.0020
σ_g	1.00128	1.0025	1.0015
ρ_g	1.00132	1.0033	1.0017
Policy and Frictions			
ρ_r	1.00142	1.0044	1.0032
ϕ_π	1.00279	1.0074	1.0045
ϕ_y	1.00238	1.0061	1.0049
ρ_τ	1.00319	1.0064	1.0058
γ_τ^b	1.00251	1.0047	1.0069
γ_τ^y	1.00238	1.0057	1.0063
λ_p	1.00315	1.0056	1.0048
λ_w	1.00229	1.0045	1.0032
ι_p	1.00244	1.0084	1.0051
ι_w	1.00214	1.0060	1.0056
χ	1.00283	1.0052	1.0053

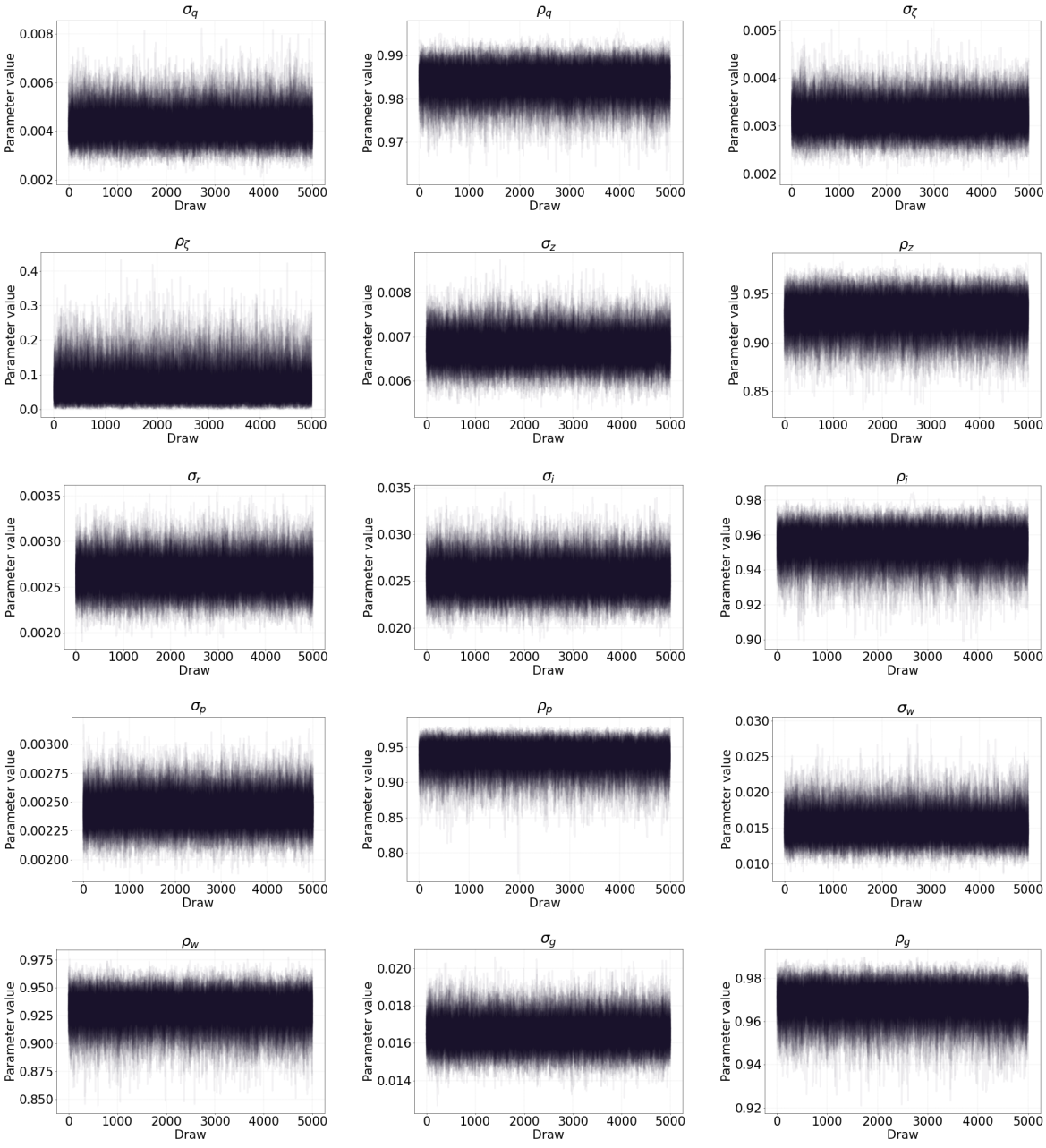
Notes: Values report the potential scale reduction factor $\hat{R}$ of Gelman and Rubin (1992) for each parameter. Values below 1.01 indicate convergence. The first column shows the statistic for the full-sample estimate, while the last two columns show the parameter estimates for the subperiods 1979 to 1999 and 2000 to 2019.

Figures 5 and 6 illustrate the trace plots of the 128 chains over 5000 draws from the posterior after a 5000 draw burn-in. Visual inspection of the trace plots indicates satisfactory mixing. For all parameters the chains feature stationary fluctuations around a stable level, no visible drift or regime shifts, as well as overlap of different chains overlap which suggests convergence. Shock standard deviations appear especially well

behaved with tight stationary bands. Autoregressive coefficients mix somewhat more slowly as expected when persistence is high. In sum the traces support reliable posterior inference.

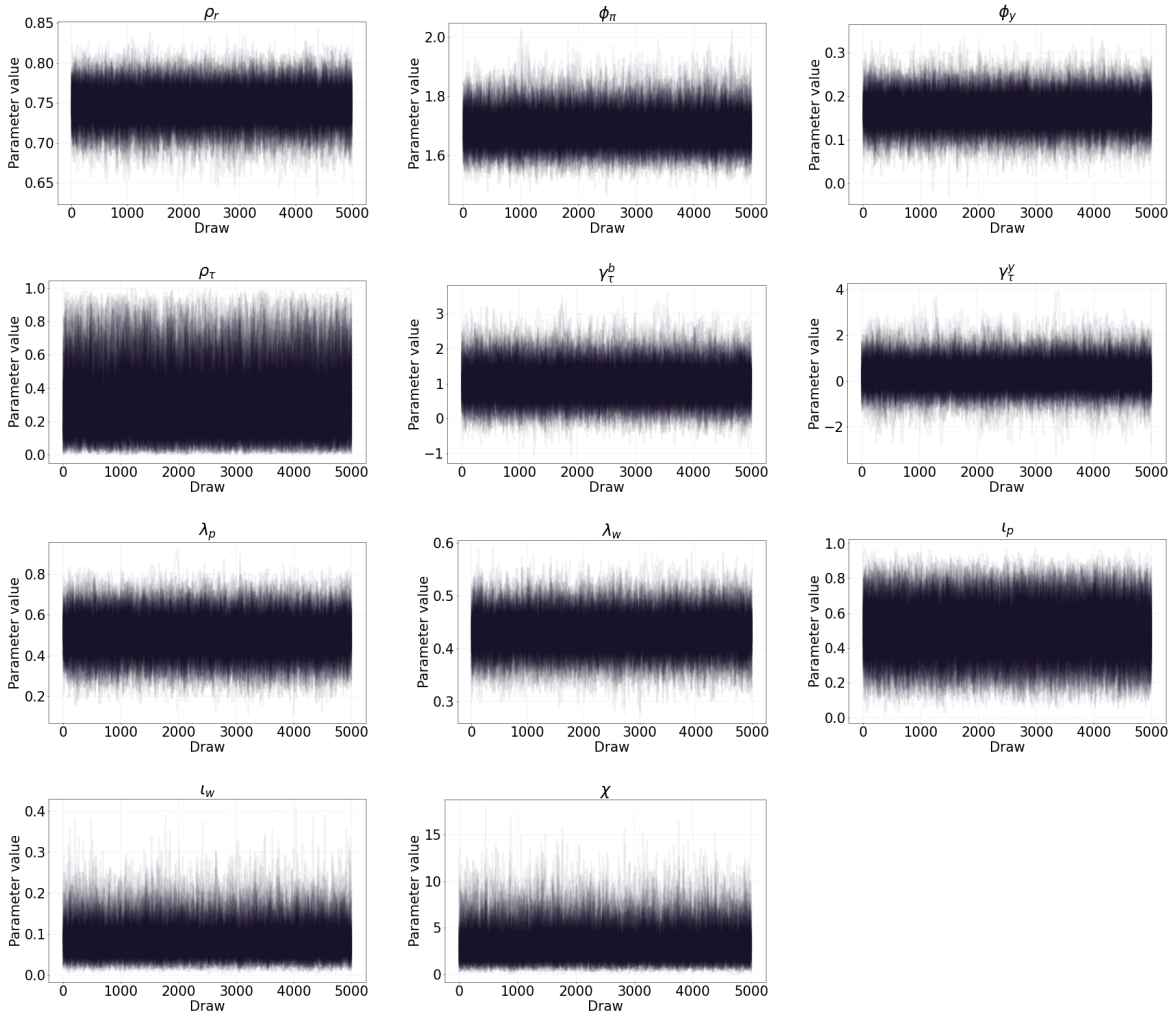
The traces for the policy parameters and frictions indicate generally satisfactory mixing after the burn-in period. The chains for ρ_r, ϕ_π, and ϕ_y fluctuate around stable centers with frequent crossovers and no visible drift, which points to convergence. The frictions λ_p, λ_w, and ι_p also show tight stationary bands and good overlap. The fiscal block is somewhat more variable: ρ_τ explores a wider interval and moves more slowly. The level parameter χ mixes the most slowly and spans the widest range, implying higher autocorrelation and a lower effective sample size relative to the others. Overall the figure supports reliable inference for most parameters, with mild caution warranted for χ and to a lesser extent for ρ_τ.

Figure 5 Traceplots for shock parameters after 5000 burn-in draws



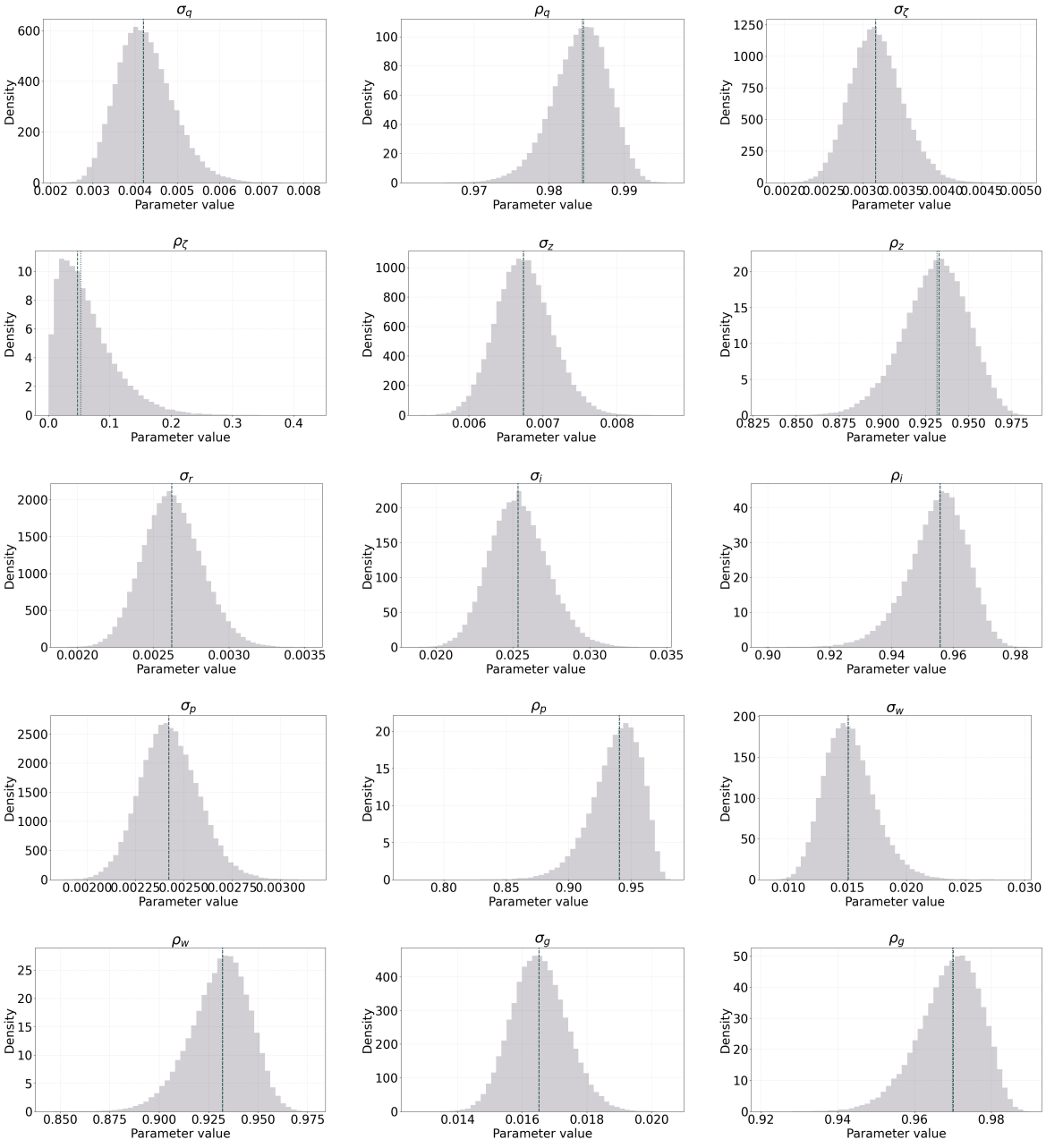
Notes: Traceplots of the 128 chains used in estimation. The traceplots only illustrates the last 5000 draws from all 128 chains. I discarded the first 5000 draws per chain as burn-in.

Figure 6 Traceplots for policy parameters and frictions after 5000 burn-in draws



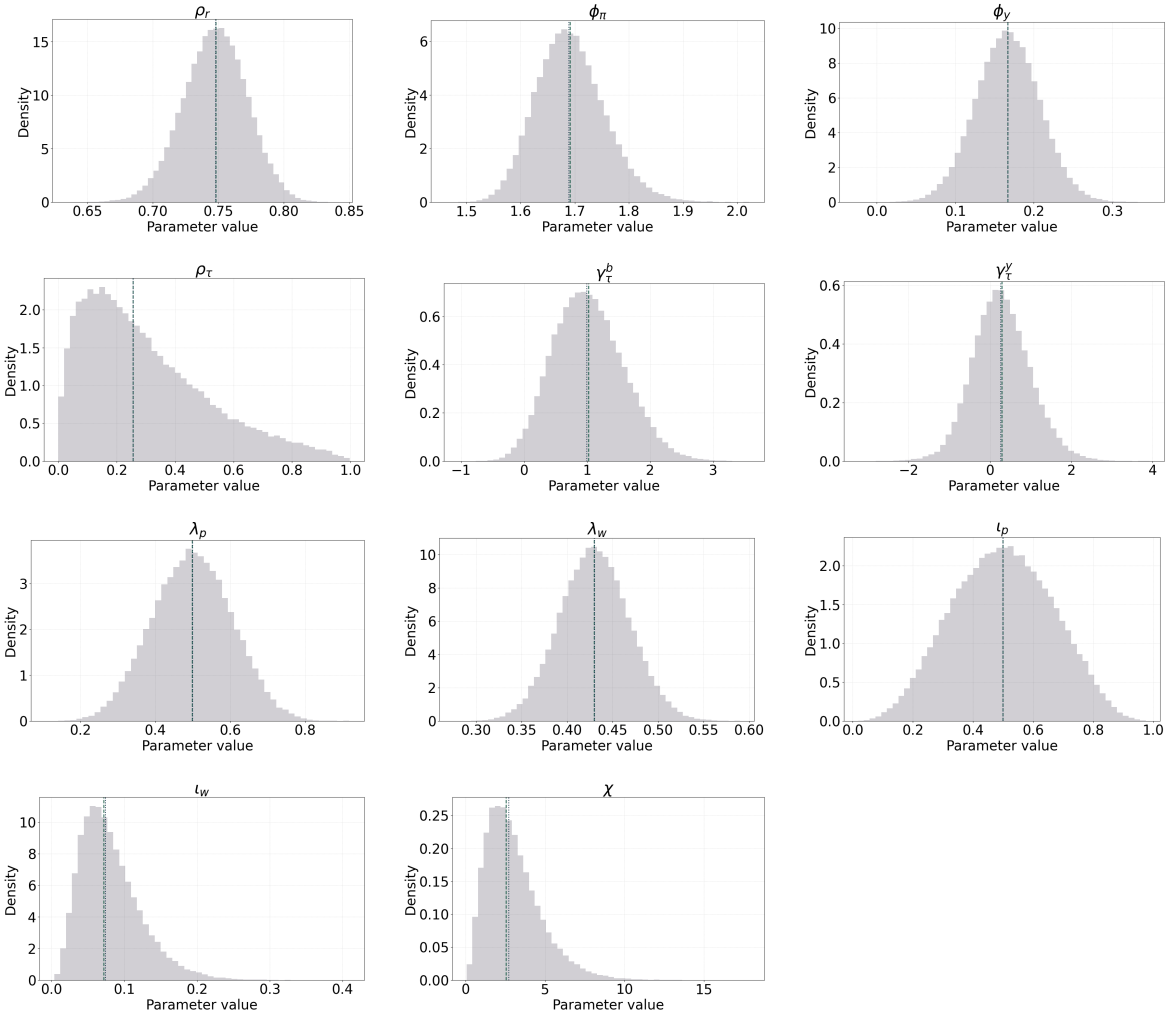
Notes: Traceplots of the 128 chains used in estimation. The traceplots only illustrates the last 5000 draws from all 128 chains. I discarded the first 5000 draws per chain as burn-in.

Figure 7 Posterior histogram of shock parameters



Notes: Posterior histogram from Bayesian estimation. The histogram only illustrates the last 5000 draws from all 128 chains. I discarded the first 5000 draws per chain as burn-in.

Figure 8 Posterior histogram of policy parameters and frictions

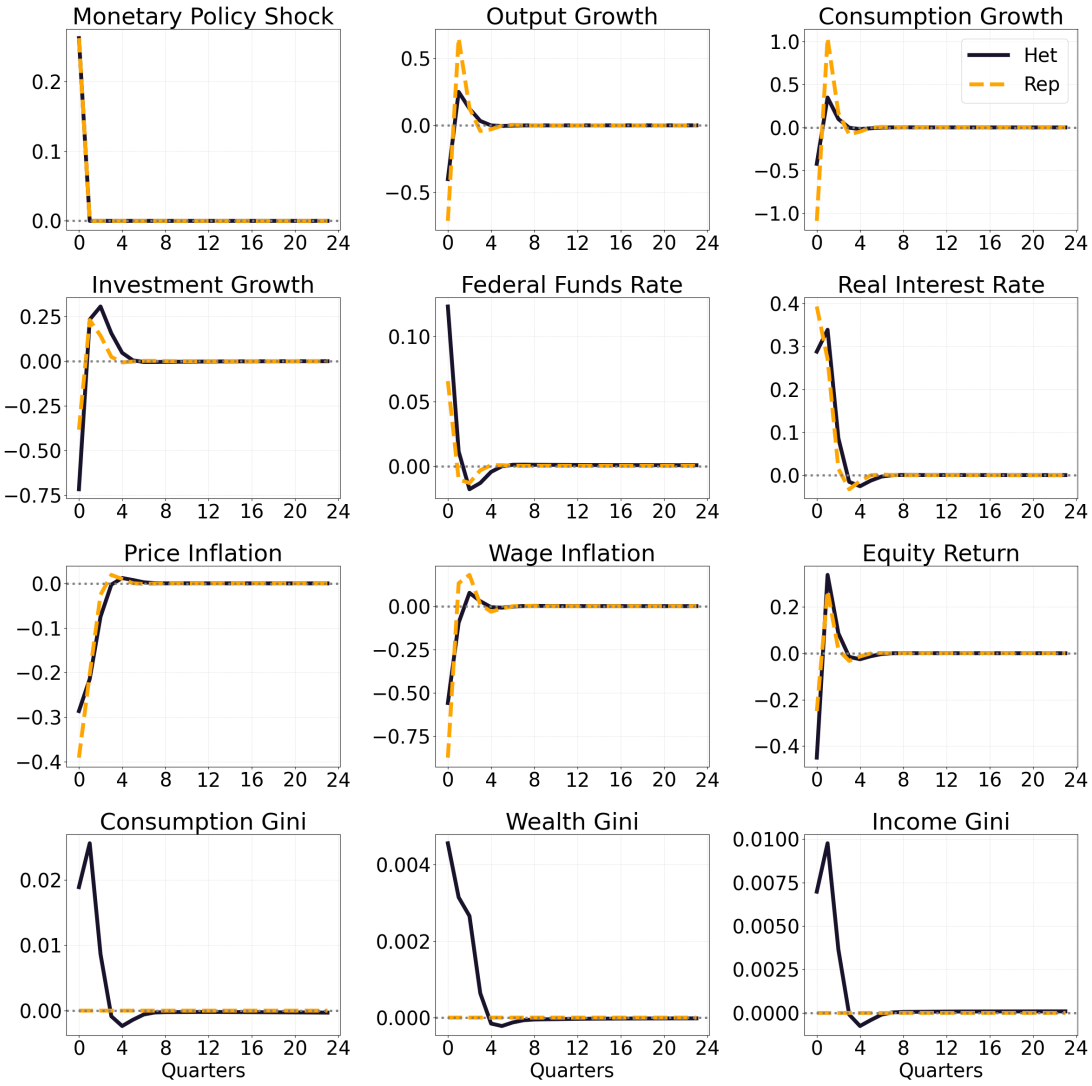


Notes: Posterior histogram from Bayesian estimation. The histogram only illustrates the last 5000 draws from all 128 chains. I discarded the first 5000 draws per chain as burn-in.

V Appendix: Structural Analysis

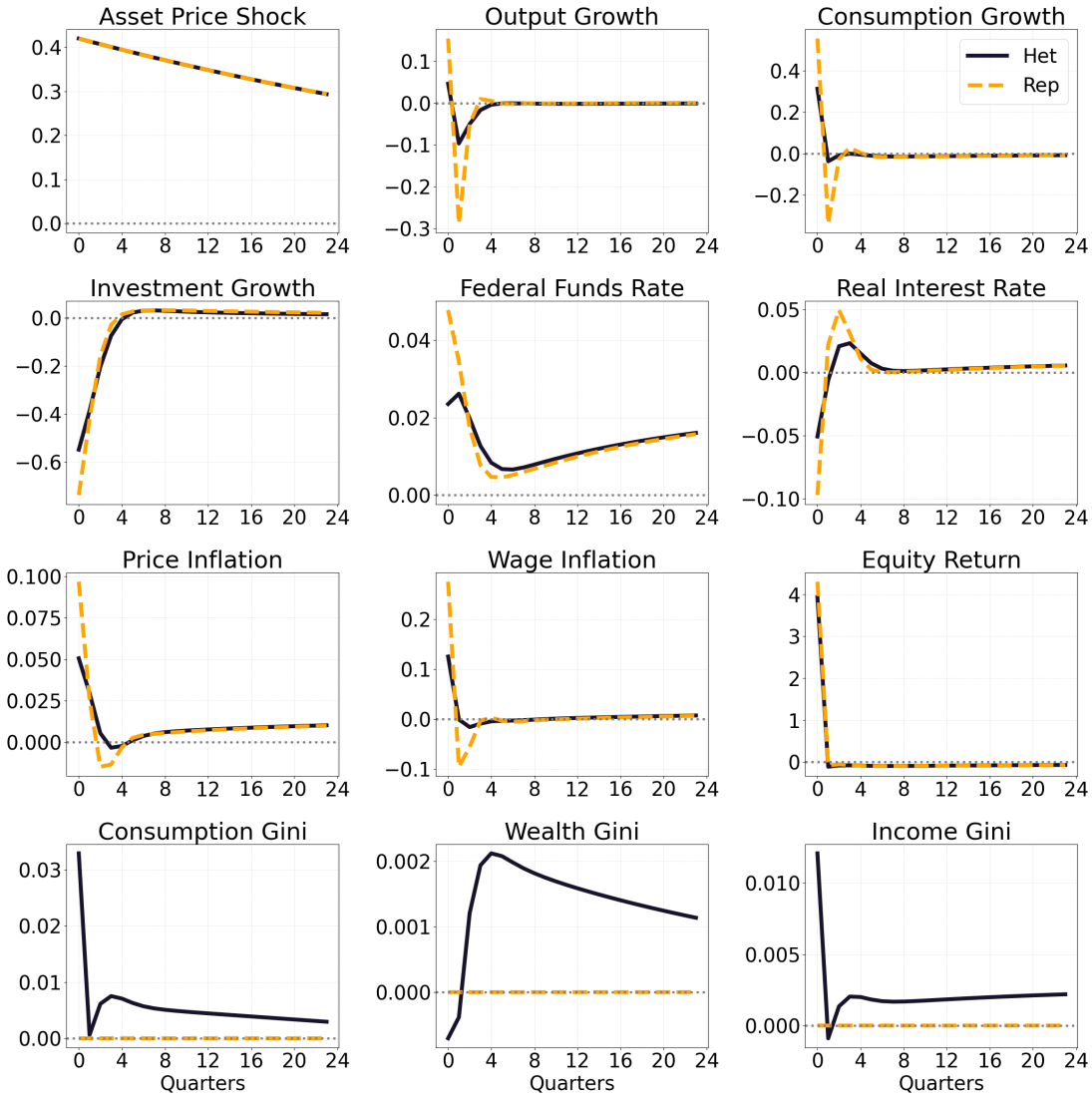
This section presents the structural results after estimation. Figures 9 to 12 show impulse responses of the estimated heterogeneous agent and representative agent models to monetary policy, asset price, investment-specific technology, and government expenditure shocks. Figure 13 reports conditional variance decompositions for all aggregate variables and Figure 14 illustrates the historical decomposition for the aggregate series.

Figure 9 Impulse response functions to a Monetary Policy Shock



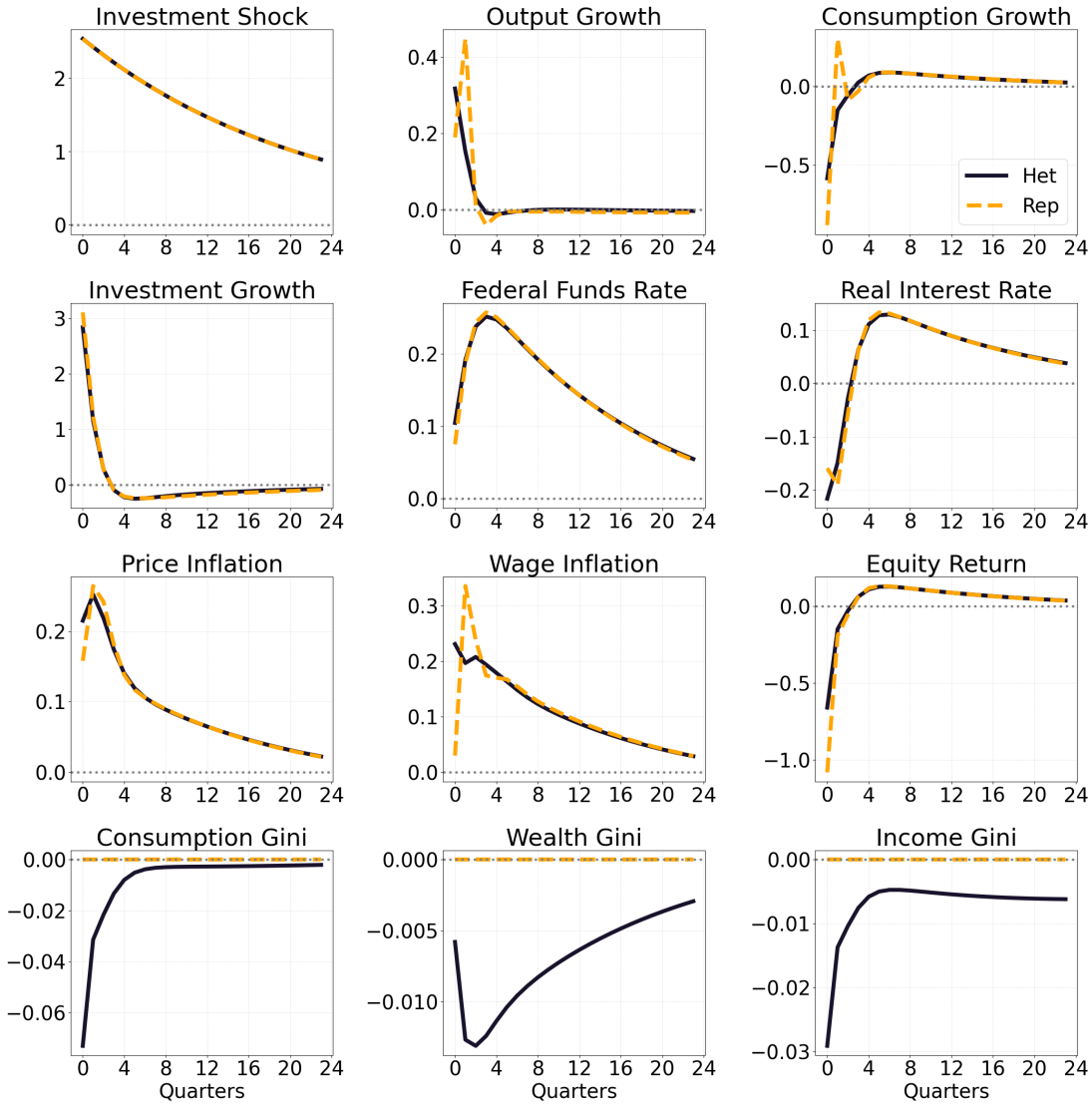
Notes: Impulse response functions (IRFs) of aggregates to monetary policy shock in the heterogeneous agent (Het) model and the representative agent (Rep) model version. The impulse responses shock absolute deviations from the steady state variable in response to the shock. The plots illustrates all responses as percentage points differences from their steady state values.

Figure 10 Impulse response functions to an Asset Price Shock



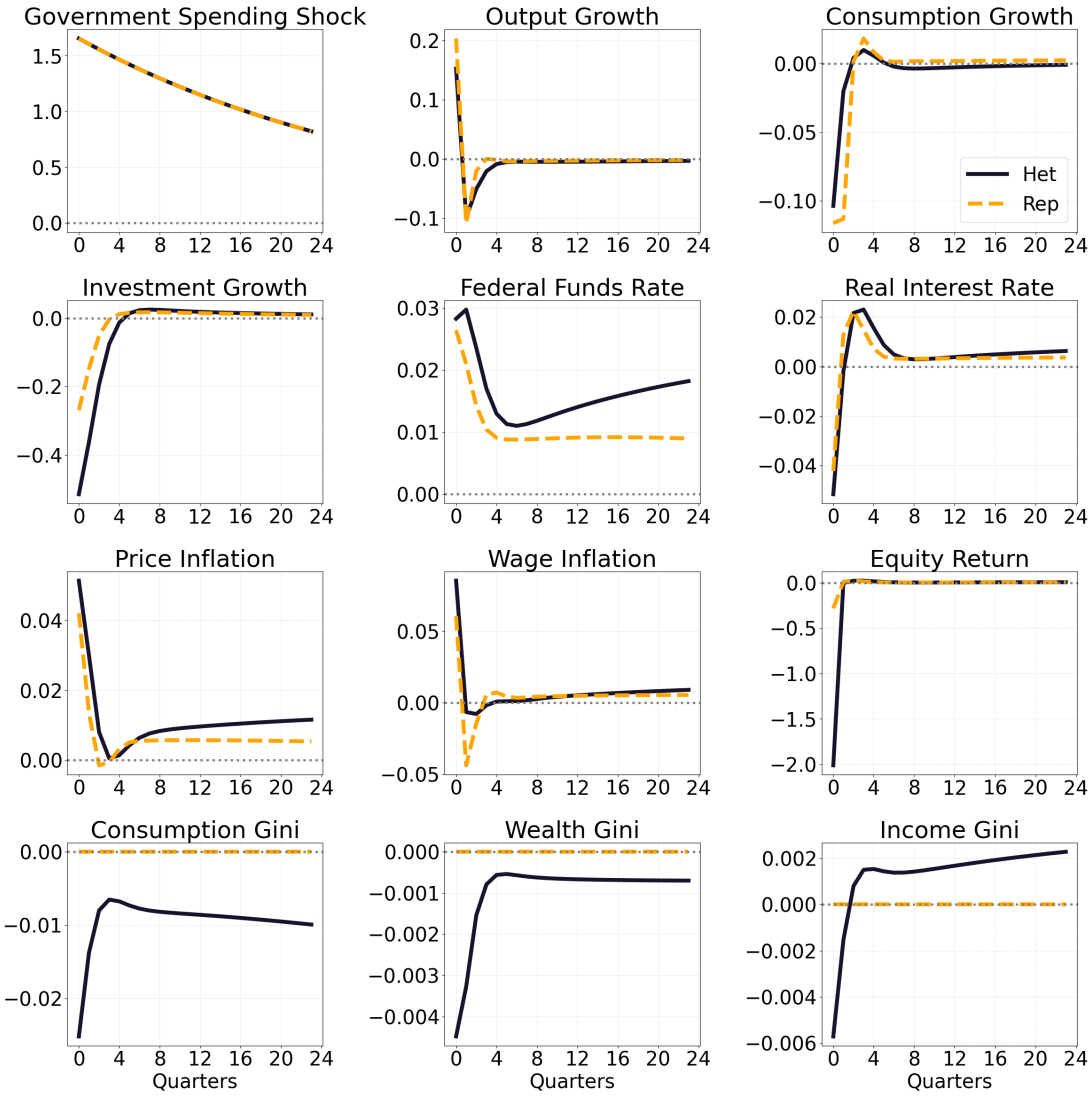
Notes: Impulse response functions (IRFs) of aggregates to monetary policy shock in the heterogeneous agent (Het) model and the representative agent (Rep) model version. The impulse responses shock absolute deviations from the steady state variable in response to the shock. The plots illustrates all responses as percentage points differences from their steady state values.

Figure 11 Impulse response functions to an Investment Specific Productivity Shock



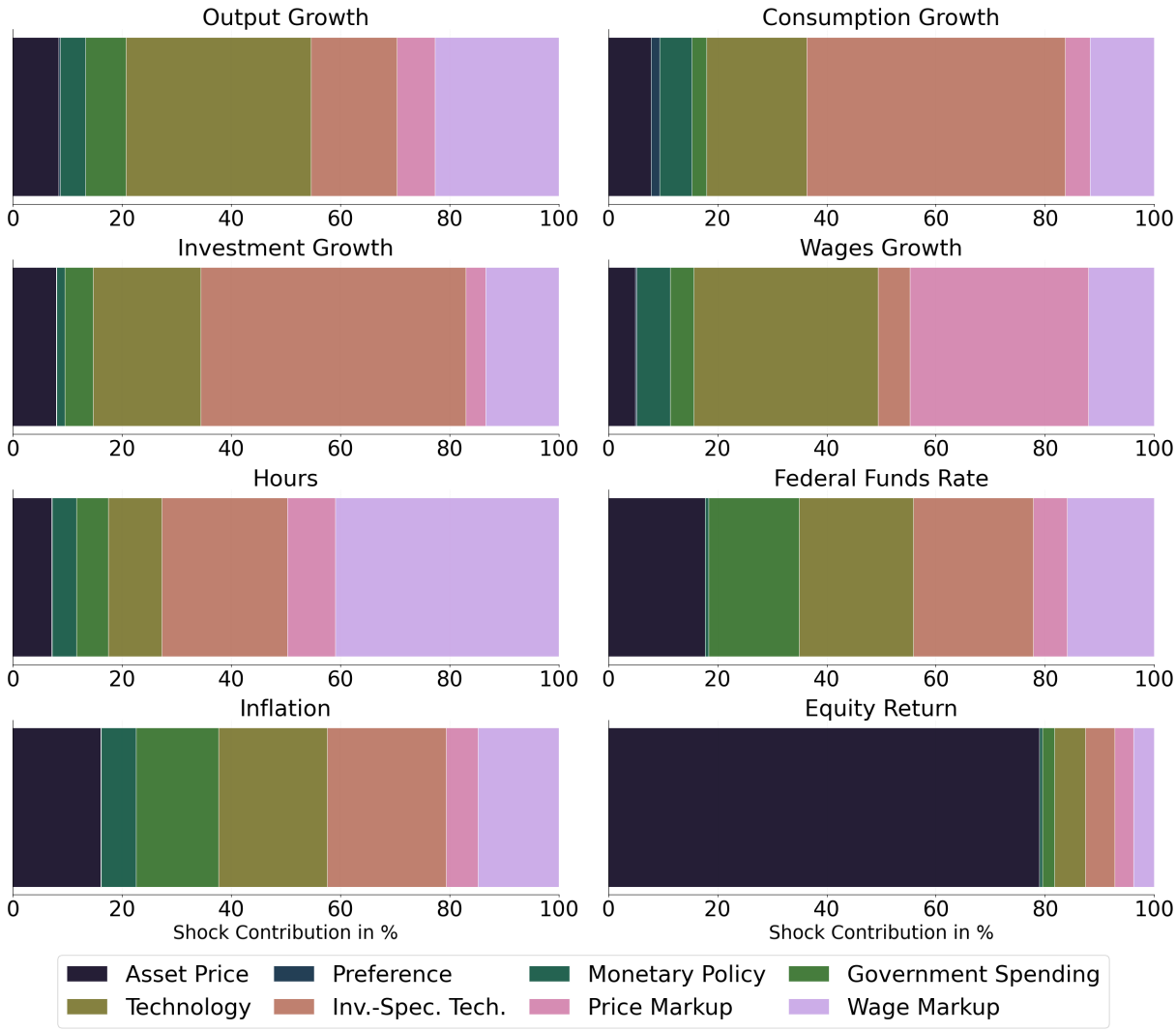
Notes: Impulse response functions (IRFs) of aggregates to an investment specific productivity shock in the heterogeneous agent (Het) model and the representative agent (Rep) model version. The impulse responses shock absolute deviations from the steady state variable in response to the shock. The plots illustrates all responses as percentage points differences from their steady state values.

Figure 12 Impulse response functions to a Government Expenditure Shock



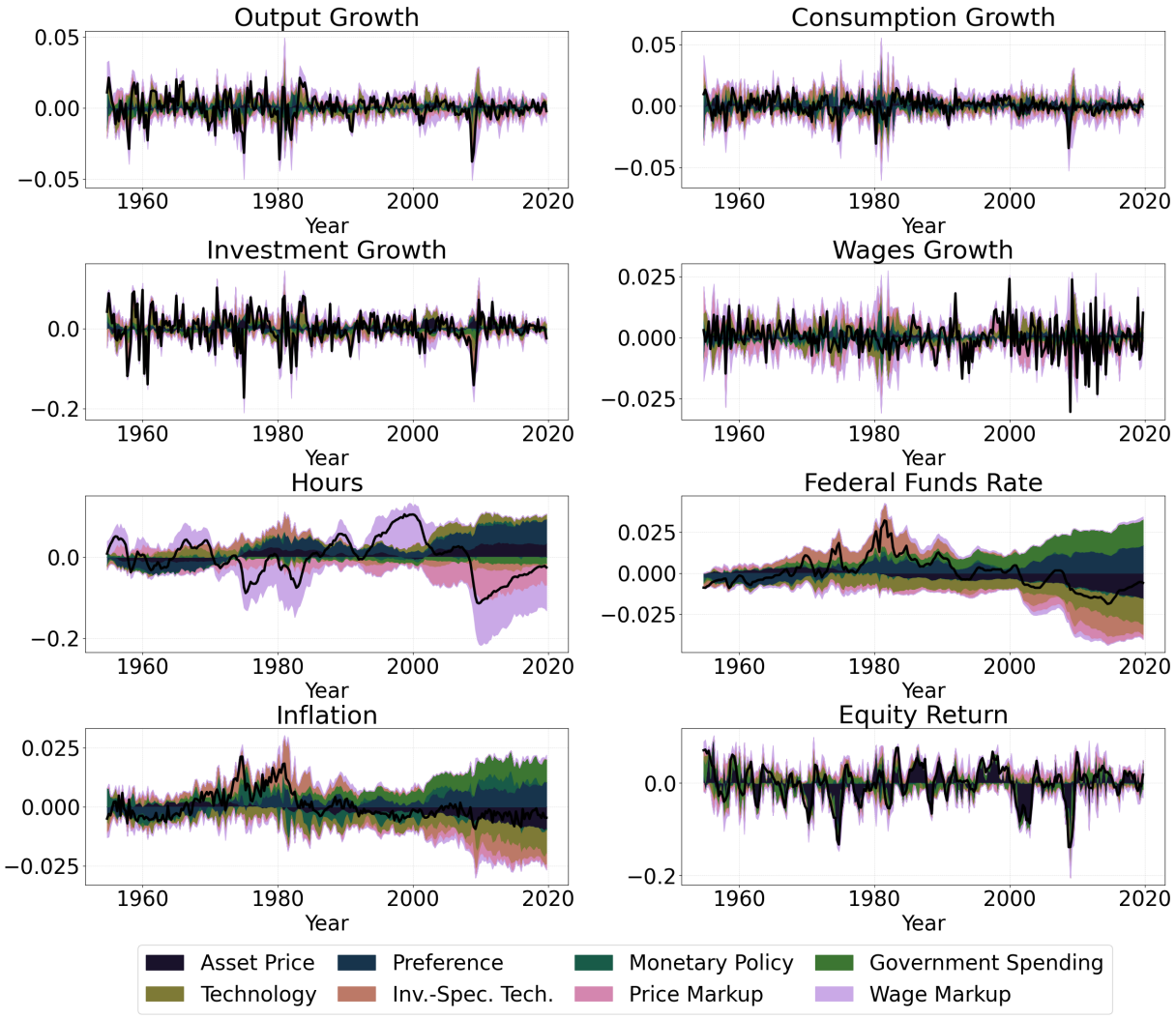
Notes: Impulse response functions (IRFs) of aggregates to a government expenditure shock in the heterogeneous agent (Het) model and the representative agent (Rep) model version. The impulse responses shock absolute deviations from the steady state variable in response to the shock. The plots illustrates all responses as percentage points differences from their steady state values.

Figure 13 Forecast Error Variance Decomposition of all Aggregate Variables



Notes: Conditional variance decompositions for the growth rates of output, consumption, investment, and wages, the log of hours, the federal funds rate, inflation, and the equity return, computed at business cycle frequencies (forecast horizon of 6 to 32 quarters) based on the estimated model. The coloured areas show the share of each variable's variance attributable to a given structural shock.

Figure 14 Historical Decomposition of Observed Variables



Notes: Historical decomposition of time-series data into the contribution of individual structual shocks.

VI Appendix: Estimates from Estimation on Subperiods

The following tables illustrate the estimated parameters from the reestimation of the model over the subperiods 1979-Q2 to 1999-Q4 and for 2000-Q1 to 2019-Q4.

Comparing parameter estimates across the full sample (1954–2019) and the two subperiods (1979–1999 and 2000–2019) reveals several systematic differences. First, the estimated shock volatilities are considerably smaller in both subperiods relative to the full sample, consistent with a calmer macroeconomic environment after the 1980s. During 1979–1999, volatilities such as σ_I, σ_z, and σ_r already decline compared to the full sample, but remain larger than in 2000–2019, where most volatilities fall further, especially for price and wage shocks, indicating a more stable nominal environment. Second, the persistence of shocks remains high across all samples but exhibits heterogeneity across types. Technology and fiscal shocks (ρ_z, ρ_g) become increasingly persistent, approaching one in the post-2000 period, while investment specific technology and policy shocks (ρ_I, ρ_r) display lower persistence in both subperiods, with the most pronounced reduction during 1979–1999.

Third monetary policy parameters evolve notably over time. The response to inflation ϕ_π rises from about 1.7 in the full sample to above 2.1 in 1979–1999 and around 2.3 in 2000–2019, suggesting a progressively stronger anti-inflation stance. The output response ϕ_y remains moderate but declines from roughly 0.17 to 0.11 after 2000, indicating a slightly weaker focus on output stabilization. The interest-rate smoothing parameter ρ_r decreases from 0.75 in the full sample to 0.60 in 1979–1999 and returns to 0.73 in 2000–2019, implying more volatile rate adjustments in the earlier period and more gradual adjustments thereafter.

Fourth, fiscal and nominal rigidities also shift across subperiods. The fiscal feedback to debt γ_τ^b strengthens markedly from about 1.0 in the full sample to 1.6 in 1979–1999 and almost 2.0 in 2000–2019, pointing to tighter fiscal discipline in both subperiods, while the output response γ_τ^y turns mildly positive only after 2000. Nominal rigidities remain broadly similar, although wage rigidity and indexation (λ_w, ι_w) decline sharply in the later period, consistent with more flexible labor markets. The adjustment cost parameter χ remains close to 2.5 across all samples, showing little sensitivity to the estimation window.

Overall, the post-2000 period is characterized by lower macroeconomic volatility, more persistent but smaller shocks, a stronger and steadier monetary response to inflation, and reduced wage rigidities. The pre-2000 period retains somewhat higher volatility and less persistent shocks, while the full-sample estimates largely average across

Table 9 Bayesian estimation results for 1979 to 1999: shock and policy parameters

		Prior		Posterior			
Shock Parameter	**Distribution**	**Mean**	**SD**	**Mean**	**Median**	**5%**	**95%**
$\sigma_q \cdot 100$	Inv. Gamma	10.0	25.0	1.368	1.371	0.922	2.022
ρ_q	Beta	0.5	0.2	0.882	0.881	0.821	0.927
$\sigma_\zeta \cdot 100$	Inv. Gamma	10.0	25.0	0.476	0.475	0.380	0.599
ρ_ζ	Beta	0.5	0.2	0.062	0.069	0.012	0.210
$\sigma_z \cdot 100$	Inv. Gamma	10.0	25.0	0.510	0.510	0.436	0.598
ρ_z	Beta	0.5	0.2	0.999	0.999	0.997	1.000
$\sigma_I \cdot 100$	Inv. Gamma	10.0	25.0	2.214	2.211	1.918	2.567
ρ_I	Beta	0.5	0.2	0.808	0.808	0.734	0.866
$\sigma_p \cdot 100$	Inv. Gamma	10.0	25.0	0.287	0.287	0.239	0.348
ρ_p	Beta	0.5	0.2	0.610	0.611	0.341	0.831
$\sigma_w \cdot 100$	Inv. Gamma	10.0	25.0	1.100	1.094	0.830	1.482
ρ_w	Beta	0.5	0.2	0.939	0.939	0.910	0.960
$\sigma_G \cdot 100$	Inv. Gamma	10.0	25.0	1.278	1.277	1.085	1.508
ρ_G	Beta	0.5	0.2	0.907	0.908	0.817	0.953
$\sigma_r \cdot 100$	Inv. Gamma	10.0	25.0	0.471	0.470	0.394	0.564

		Prior		Posterior			
Policy Parameter	**Distribution**	**Mean**	**SD**	**Mean**	**Median**	**5%**	**95%**
ρ_r	Beta	0.5	0.2	0.599	0.601	0.522	0.668
ϕ_π	Gamma	1.5	0.3	2.156	2.154	1.925	2.421
ϕ_Y	Normal	0.1	0.1	0.169	0.169	0.092	0.245
ρ_τ	Beta	0.5	0.2	0.436	0.445	0.100	0.825
γ_τ^B	Normal	0.0	1.0	1.622	1.622	0.752	2.494
γ_τ^Y	Normal	0.0	1.0	-0.005	-0.010	-1.494	1.489
λ_p	Beta	0.5	0.1	0.500	0.500	0.329	0.672
λ_w	Beta	0.5	0.1	0.456	0.457	0.378	0.533
ι_p	Beta	0.5	0.2	0.501	0.501	0.228	0.773
ι_w	Beta	0.5	0.2	0.340	0.340	0.137	0.626
χ	Gamma	4.0	2.0	2.524	2.669	0.837	6.298

Notes: Posterior estimates use the same priors as in the full sample. Reported values are posterior means, medians and 90 percent credible intervals. Shock standard deviations are scaled by 100 to enhance readability.

these two regimes, reflecting the transition from a high-volatility to a low-volatility macroeconomic environment.

Finally, I examine the volatility of aggregate variables at business cycle frequencies across the two subperiods. Table 11 reports the variances of key aggregates, computed using the posterior mean estimates for each period. For all variables considered, the

Table 10 Bayesian estimation results for 2000 to 2019: shock and policy parameters

		Prior		Posterior			
Shock Parameter	**Distribution**	**Mean**	**SD**	**Mean**	**Median**	**5%**	**95%**
$\sigma_q \cdot 100$	Inv. Gamma	10.0	25.0	1.036	1.033	0.719	1.504
ρ_q	Beta	0.5	0.2	0.941	0.940	0.908	0.962
$\sigma_\zeta \cdot 100$	Inv. Gamma	10.0	25.0	0.443	0.443	0.351	0.558
ρ_ζ	Beta	0.5	0.2	0.065	0.073	0.013	0.206
$\sigma_z \cdot 100$	Inv. Gamma	10.0	25.0	0.556	0.556	0.462	0.668
ρ_z	Beta	0.5	0.2	0.955	0.954	0.900	0.982
$\sigma_I \cdot 100$	Inv. Gamma	10.0	25.0	1.548	1.543	1.245	1.948
ρ_I	Beta	0.5	0.2	0.902	0.902	0.807	0.955
$\sigma_p \cdot 100$	Inv. Gamma	10.0	25.0	0.363	0.362	0.308	0.430
ρ_p	Beta	0.5	0.2	0.877	0.875	0.799	0.931
$\sigma_w \cdot 100$	Inv. Gamma	10.0	25.0	3.803	3.764	2.709	5.530
ρ_w	Beta	0.5	0.2	0.951	0.950	0.920	0.971
$\sigma_G \cdot 100$	Inv. Gamma	10.0	25.0	1.331	1.330	1.153	1.543
ρ_G	Beta	0.5	0.2	0.993	0.992	0.987	0.996
$\sigma_r \cdot 100$	Inv. Gamma	10.0	25.0	0.292	0.292	0.244	0.353

		Prior		Posterior			
Policy Parameter	**Distribution**	**Mean**	**SD**	**Mean**	**Median**	**5%**	**95%**
ρ_r	Beta	0.5	0.2	0.730	0.731	0.664	0.786
ϕ_π	Gamma	1.5	0.3	2.314	2.310	2.033	2.647
ϕ_Y	Normal	0.1	0.1	0.114	0.114	0.036	0.191
ρ_τ	Beta	0.5	0.2	0.231	0.238	0.043	0.633
γ_τ^B	Normal	0.0	1.0	1.955	1.928	0.879	3.119
γ_τ^Y	Normal	0.0	1.0	0.629	0.620	-0.735	2.021
λ_p	Beta	0.5	0.1	0.500	0.500	0.328	0.671
λ_w	Beta	0.5	0.1	0.231	0.233	0.165	0.308
ι_p	Beta	0.5	0.2	0.499	0.500	0.227	0.771
ι_w	Beta	0.5	0.2	0.222	0.223	0.082	0.473
χ	Gamma	4.0	2.0	2.541	2.692	0.846	6.303

Notes: Posterior estimates are based on Bayesian inference using the same priors as in the full sample. Reported values are posterior means, medians, and 90 percent credible intervals. Shock standard deviations are scaled by 100 to enhance readability.

standard deviations decline from the first to the second subperiod.

Table 11 Variation of variables at business cycle frequencies for the two subperiods

Variable	1979-1999	2000-2019
$100\sigma(y)$	4.15	1.36
$100\sigma(c)$	1.39	0.58
$100\sigma(\pi)$	6.10	4.33
$100\sigma(r^{eq})$	7.57	6.07
$100\sigma(r^{1y})$	1.03	0.32
$100\sigma(r^{10y})$	1.43	0.56

Notes: Volatility of aggregate variables over the business cycle frequency computed (6 - 32 quarters) with the posterior mean parameters of the estimated heterogeneous agent model for the respective sample periods. The variance over the business cycle frequency is computed based on Uhlig (2001) and scaled by 100 for better readability.

VII Appendix: The Impact of Monetary Policy on Asset Premia

Table 12 illustrates the impact that monetary policy stance has on asset premia for more assets, as well as lists the variance of more aggregate variables. For all assets considered, the picture remains identical. More aggressive inflation stabilization (higher ϕ_π) leads to higher variance in all variables, with exception of inflation, and increases all asset premia. Stronger output stabilization (higher ϕ_y) reduces the volatility of all aggregate variables, and reduces all asset premia, with the only exception being the 10-year term premium, which increases again from 1.71 to 1.72 percent in the last two columns.

Table 12 Annualized Asset Premia under varying Monetary Policy Stance

	Coefficient for Inflation (ϕ_π)			**Coefficient for Output** (ϕ_y)		
Premia	$\phi_\pi = 1.1$	$\phi_\pi = 1.69$	$\phi_\pi = 3.0$	$\phi_y = 0.0$	$\phi_y = 0.17$	$\phi_y = 0.5$
Equity	4.37	4.92	5.28	5.02	4.92	4.77
Bond 6m	0.07	0.07	0.12	0.09	0.07	0.04
Bond 1y	0.17	0.24	0.34	0.27	0.24	0.21
Bond 2y	0.36	0.64	0.82	0.66	0.64	0.62
Bond 5y	0.64	1.26	1.54	1.27	1.26	1.26
Bond 10y	0.83	1.71	2.07	1.72	1.71	1.72
Bond 20y	0.92	2.01	2.45	2.04	2.01	1.99
Std. Dev.	$\phi_\pi = 1.1$	$\phi_\pi = 1.69$	$\phi_\pi = 3.0$	$\phi_y = 0.0$	$\phi_y = 0.17$	$\phi_y = 0.5$
$100\sigma(y)$	1.06	1.07	1.17	1.09	1.07	1.03
$100\sigma(c)$	0.53	0.55	0.61	0.56	0.55	0.53
$100\sigma(\pi)$	3.12	2.08	1.14	6.14	6.12	6.10
$100\sigma(r^{eq})$	6.10	6.12	6.20	2.16	2.08	1.94
$100\sigma(r^{1y})$	0.24	0.20	0.24	0.21	0.20	0.19
$100\sigma(r^{10y})$	0.72	0.75	0.81	0.76	0.75	0.75

Notes: Annualized premia and volatility over the business cycle frequency computed with the posterior mean parameters of the estimated heterogeneous agent model for the full sample period. The table varies the monetary policy responses to inflation ϕ_π and output ϕ_y. Premia are computed following Auclert et al. (2024): $\frac{R_1 - R_0}{R} \approx -X\,\bar{\lambda}\,\sigma^2$, where X denotes the ex post variation of an asset's excess return relative to the three month bond and $\bar{\lambda}$ denotes the aggregate pricing kernel. The variance over the business cycle frequency is computed based on Uhlig (2001).